

Today 7.2

L22



Today 7.2

L22

Elastic  
potential  
energy

Today 7.2  
Monday 7.3 & 7.4

L22



Today 7.2

L22

Monday 7.3 & 7.4

Conservative  
& non-conservative  
forces

Today 7.2

L22

Monday 7.3 & 7.4

Force &  
potential  
energy

# Elastic potential energy

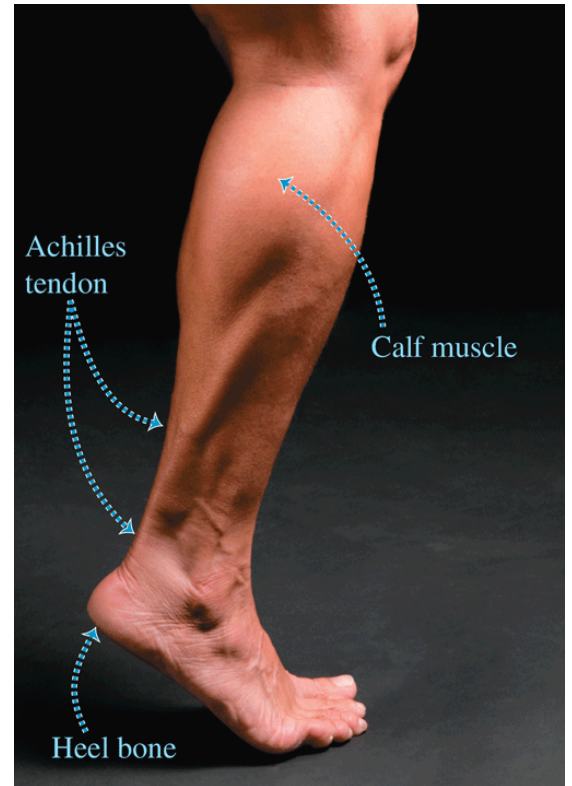
# Elastic potential energy

Storage of energy in a deformable object such as a spring or rubber band

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Tendon  
acts  
like  
natural a  
spring →



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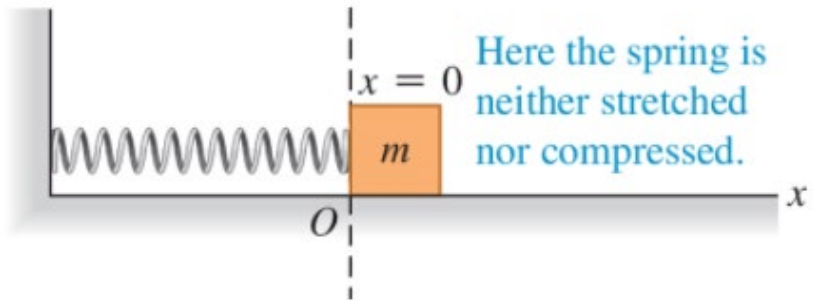
The elastic potential energy is contained in the elastic medium

The gravitational potential energy is a shared property

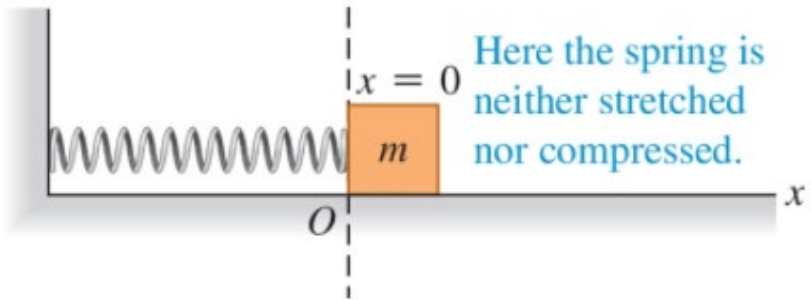
But the elastic potential energy is not shared.

The elastic potential energy is contained in the elastic medium (e.g. spring)

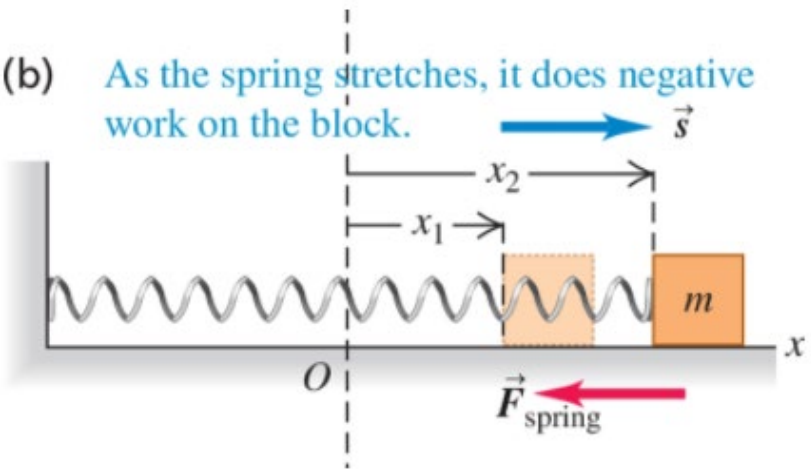
(a)



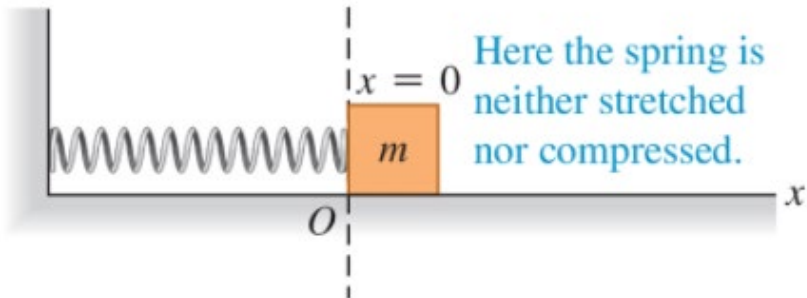
(a)



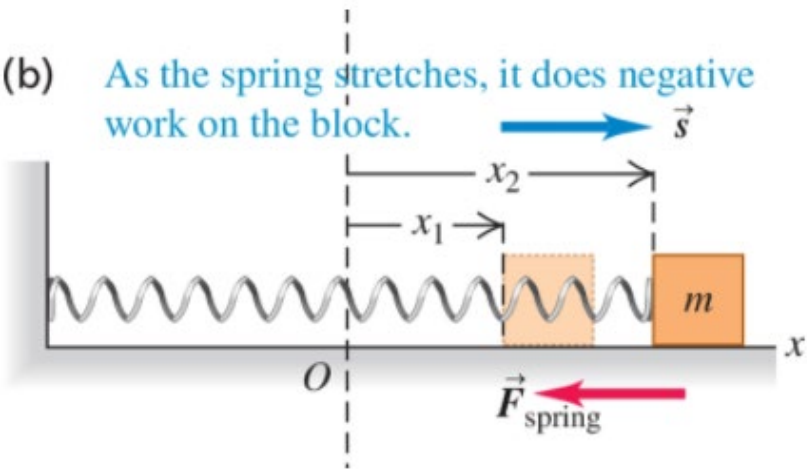
(b) As the spring stretches, it does negative work on the block.



(a)

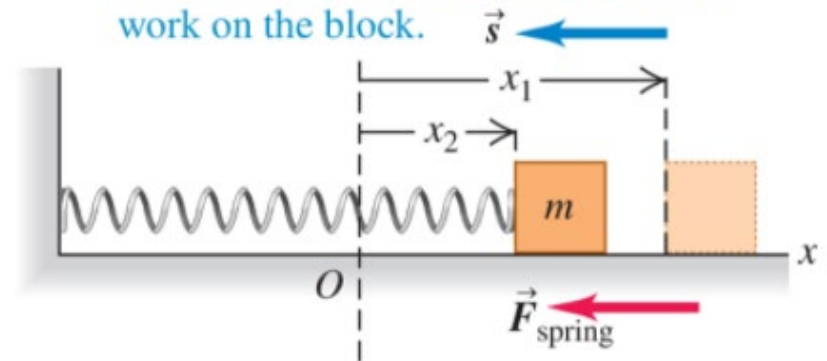


(b)

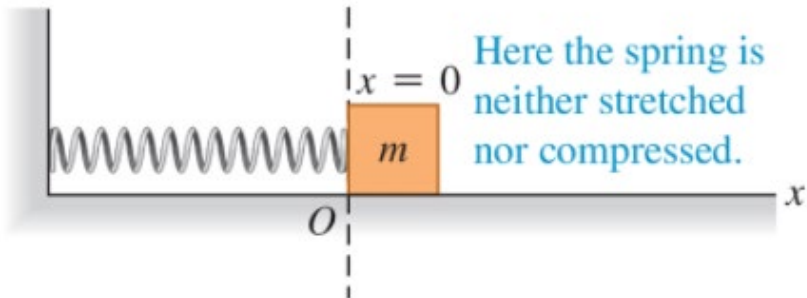


(c)

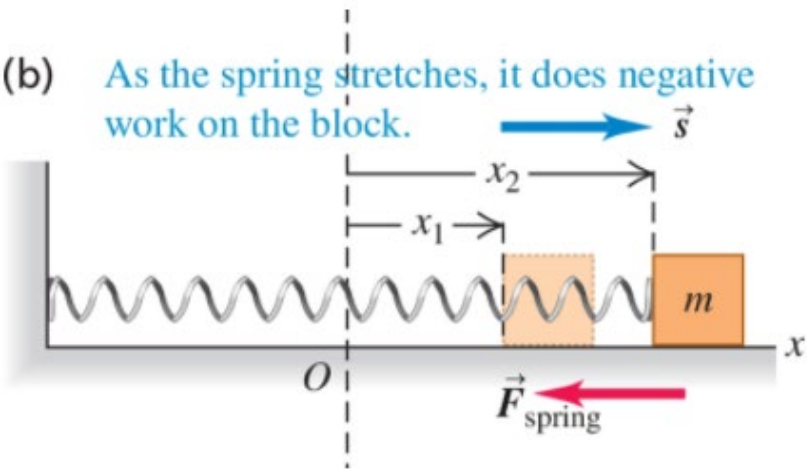
As the spring relaxes, it does positive work on the block.



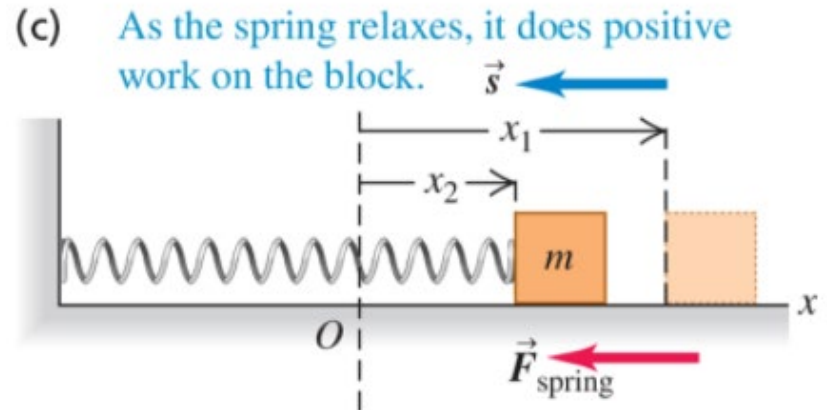
(a)



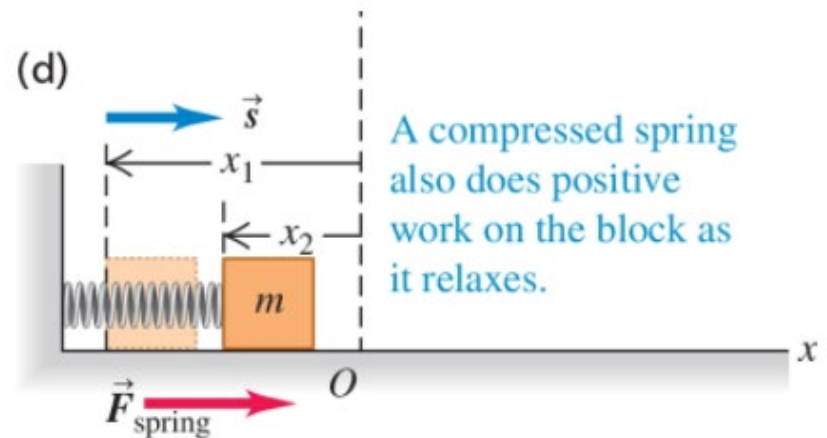
(b)



(c)



(d)



Previously we found that the work done on a spring is

$$W = \frac{1}{2}k(x_2^2 - x_1^2) \text{ , work on spring}$$

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$$U = -W \text{ then } U_{\text{el}} = \frac{1}{2}kx^2$$

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spring-force constant

→ elongation of spring

Elastic potential energy stored in spring

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spring-force constant

$$U_{el} = \frac{1}{2} k x^2$$

elongation of spring

( $x > 0$  if stretched,  
 $x < 0$  if compressed)

Elastic potential energy stored in spring

$$W_{\text{el}} = \frac{1}{2}kx_1^2 - \frac{1}{2}kx_2^2 = U_{\text{el},1} - U_{\text{el},2} = -\Delta U_{\text{el}}$$

Work done by the elastic force ...

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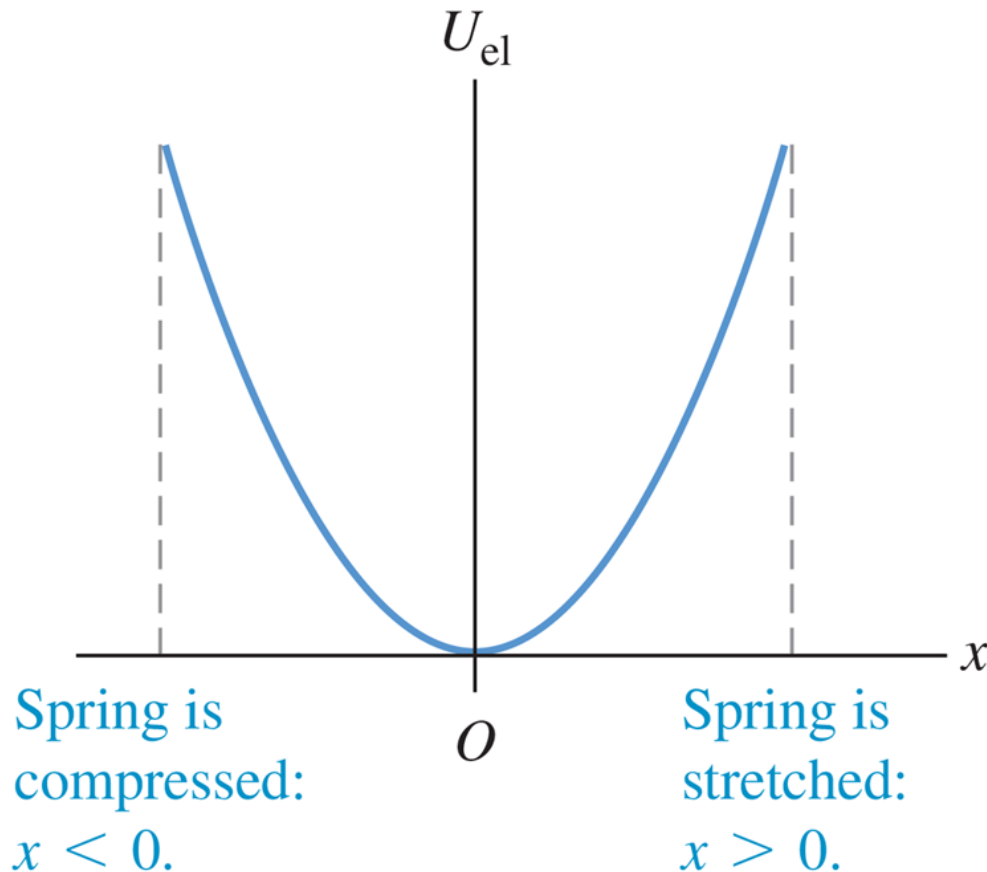
Initial and final elongations of spring

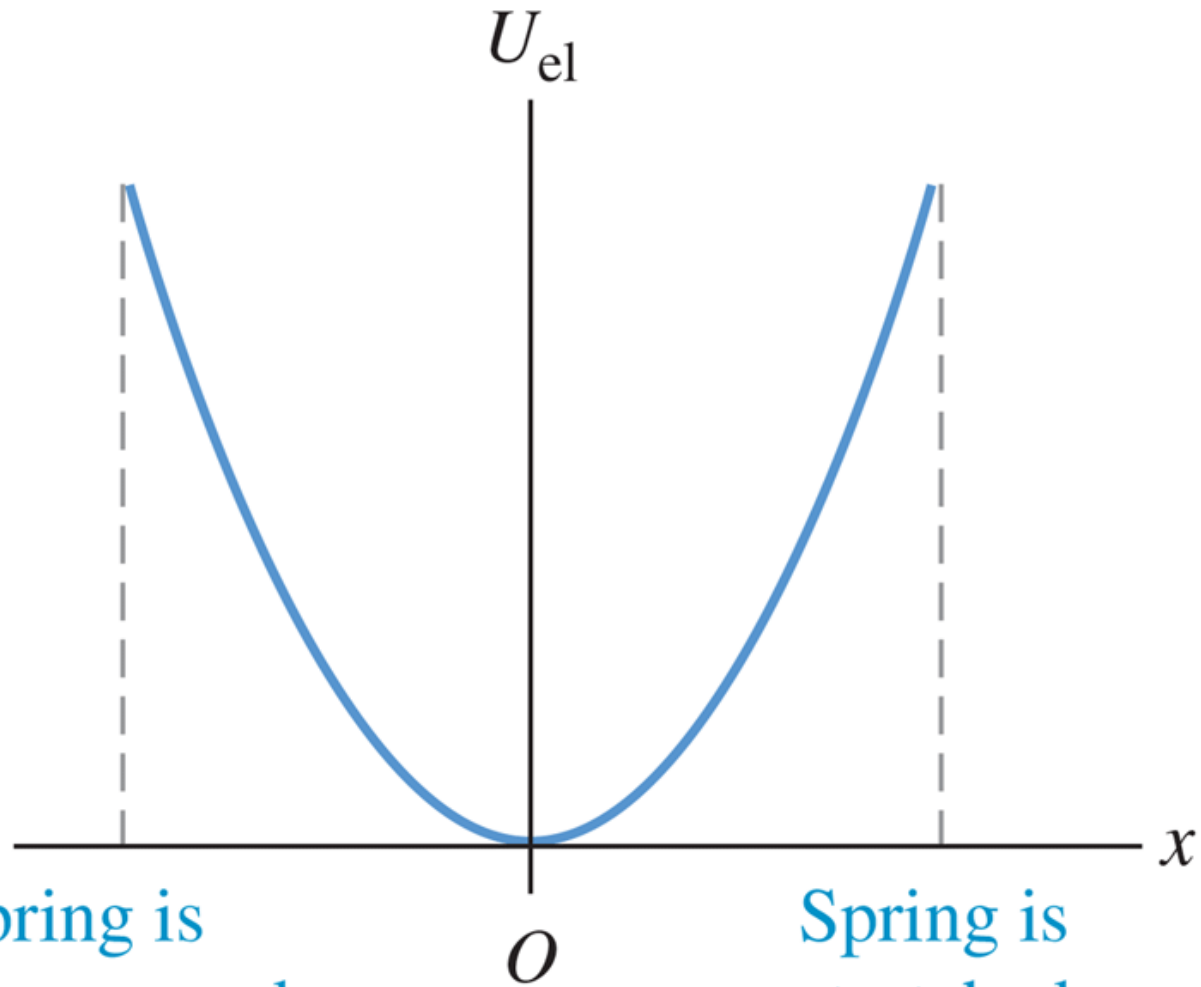
Work done by the elastic force ... equals the negative of the change in elastic potential energy.

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Force constant of spring

Initial and final elongations of spring





Spring is  
compressed:  
 $x < 0$ .

Spring is  
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 $x > 0$ .

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# Conservation of energy

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§

$$E_{tot} = K + U_{el}$$

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Or more simply

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Or more simply

$$K_1 + U_1 + W_{\text{other}} = K_2 + U_2$$

**Gravitational potential energy increases as jumper ascends.**

**Kinetic energy increases as jumper moves faster.**

**Elastic potential energy increases when trampoline is stretched.**



A glider with mass  $m = 0.200$  kg sits on a frictionless, horizontal air track, connected to a spring with force constant  $k = 5.00$  N/m. You pull on the glider, stretching the spring 0.100 m, and release it from rest. The glider moves back toward its equilibrium position ( $x = 0$ ). What is its  $x$ -velocity when  $x = 0.080$  m?

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$$\Rightarrow v_2 = \left[ \frac{k}{m} (x_1^2 - x_2^2) \right]^{1/2} = \left[ \frac{5}{0.2} \left( \frac{1}{100} - 0.08^2 \right) \right]^{1/2} \frac{m}{s}$$

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What is its  $x$ -velocity when  $x = 0.080$  m?  $m = 0.2$  kg,  $k = 5$  N/m,  $x_1 = 0.1$  m

$v_1 = 0$  Find  $v_2$  at  $x_2 = 0.08$  m:

~~$K_1 + U_1 = K_2 + U_2 \Rightarrow K_2 = U_1 - U_2$ , where~~

$$K_2 = \frac{1}{2} m v_2^2, \quad U_1 = \frac{1}{2} k x_1^2 \quad \& \quad U_2 = \frac{1}{2} k x_2^2$$

$$\Rightarrow \frac{1}{2} m v_2^2 = \frac{1}{2} k x_1^2 - \frac{1}{2} k x_2^2 \Rightarrow v_2^2 = \left(\frac{k}{m}\right) (x_1^2 - x_2^2)$$

$$\Rightarrow v_2 = \left[ \frac{k}{m} (x_1^2 - x_2^2) \right]^{1/2} = \left[ \frac{5}{0.2} (0.1^2 - 0.08^2) \right]^{1/2} \frac{m}{s}$$

$$\Rightarrow v_2 = 0.3 \frac{m}{s}$$

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$\Rightarrow v_2 = \left[\frac{k}{m}(x_1^2 - x_2^2)\right]^{1/2} = \left[\frac{5}{0.2} \left(\frac{1}{100} - 0.08^2\right)\right]^{1/2} \frac{m}{s}$

$\Rightarrow v_2 = 0.3 \frac{m}{s}$  could be + or -



Suppose the glider in **Example 7.7** is initially at rest at  $x = 0$ , with the spring unstretched. You then push on the glider with a constant force  $\vec{F}$  (magnitude 0.610 N) in the  $+x$ -direction. What is the glider's velocity when it has moved to  $x = 0.100$  m?

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$$x_i = 0, \quad \vec{F} = \hat{i}0.610\text{N}$$

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$$x_1 = 0, \quad \vec{F} = \hat{i}0.610\text{N}$$

Find  $v_2$  when  $x_2 = 0.1\text{m}$

Suppose the glider in **Example 7.7** is initially at rest at  $x = 0$ , with the spring unstretched. You then push on the glider with a constant force  $\vec{F}$  (magnitude 0.610 N) in the  $+x$ -direction. What is the glider's velocity when it has moved to  $x = 0.100$  m?  $v_1 = 0$ ,

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Find  $v_2$  when  $x_2 = 0.1\text{m}$ :

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$$\Rightarrow V_2 = \left[ \frac{2F}{m}x_2 - \frac{k}{m}x_2^2 \right]^{\frac{1}{2}} = \left[ \frac{1.22}{0.2} * 0.1 - \frac{5}{0.2} * 0.1^2 \right]^{\frac{1}{2}}$$

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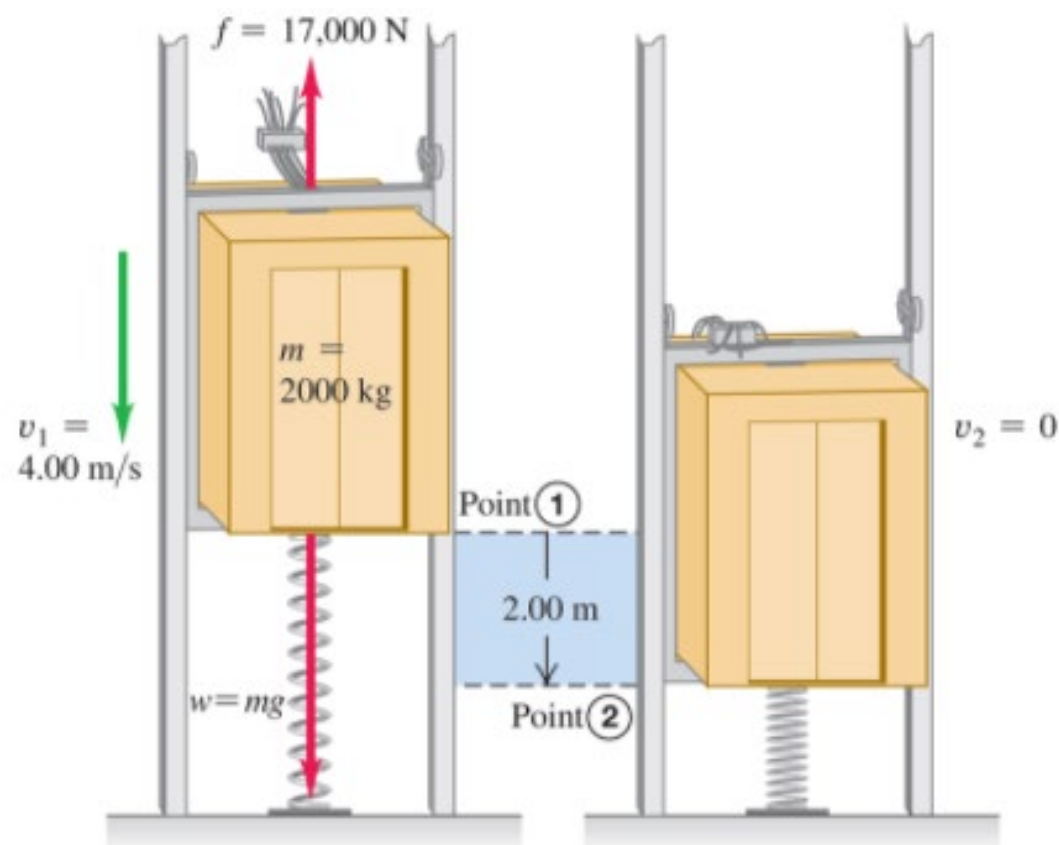
$$W_{\text{other}} = F(x_2 - \cancel{x_1}), \quad K_2 = \frac{1}{2}mV_2^2 \quad \& \quad U_2 = \frac{1}{2}kx_2^2$$

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$$\Rightarrow V_2 = \left[ \frac{2F}{m}x_2 - \frac{k}{m}x_2^2 \right]^{1/2} = \left[ \frac{1.22}{0.2} * 0.1 - \frac{5}{0.2} * 0.1^2 \right]^{1/2} \frac{\text{m}}{\text{s}}$$

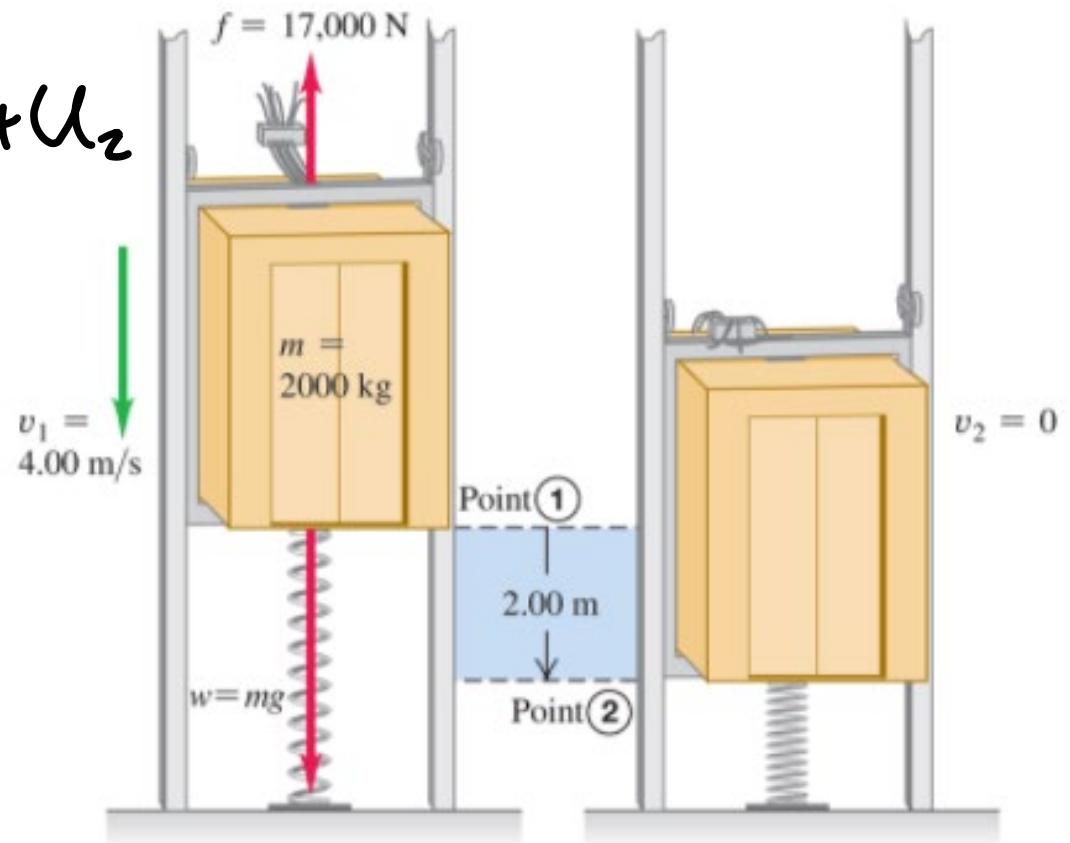
$$\Rightarrow V_2 = 0.591 \text{ m/s}$$

A 2000 kg (19,600 N) elevator with broken cables in a test rig is falling at 4.00 m/s when it contacts a cushioning spring at the bottom of the shaft. The spring is intended to stop the elevator, compressing 2.00 m as it does so (Fig. 7.17). During the motion a safety clamp applies a constant 17,000 N friction force to the elevator. What is the necessary force constant  $k$  for the spring?



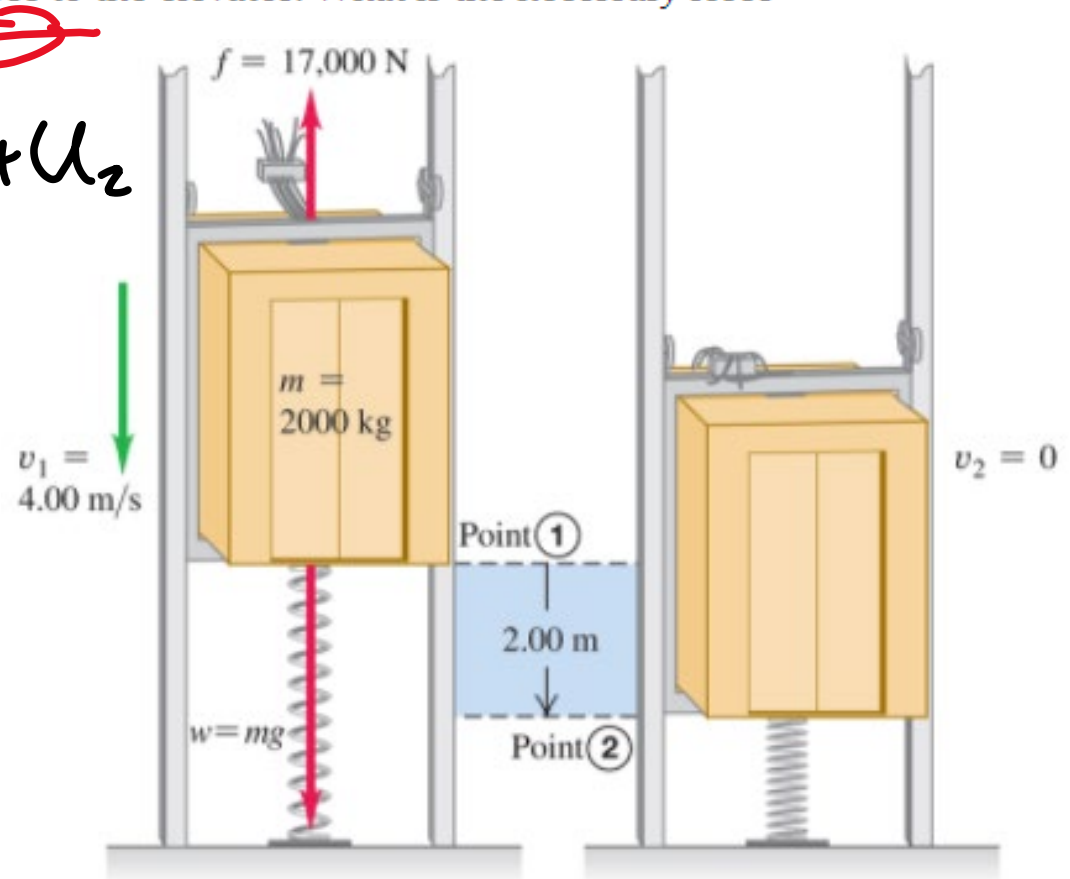
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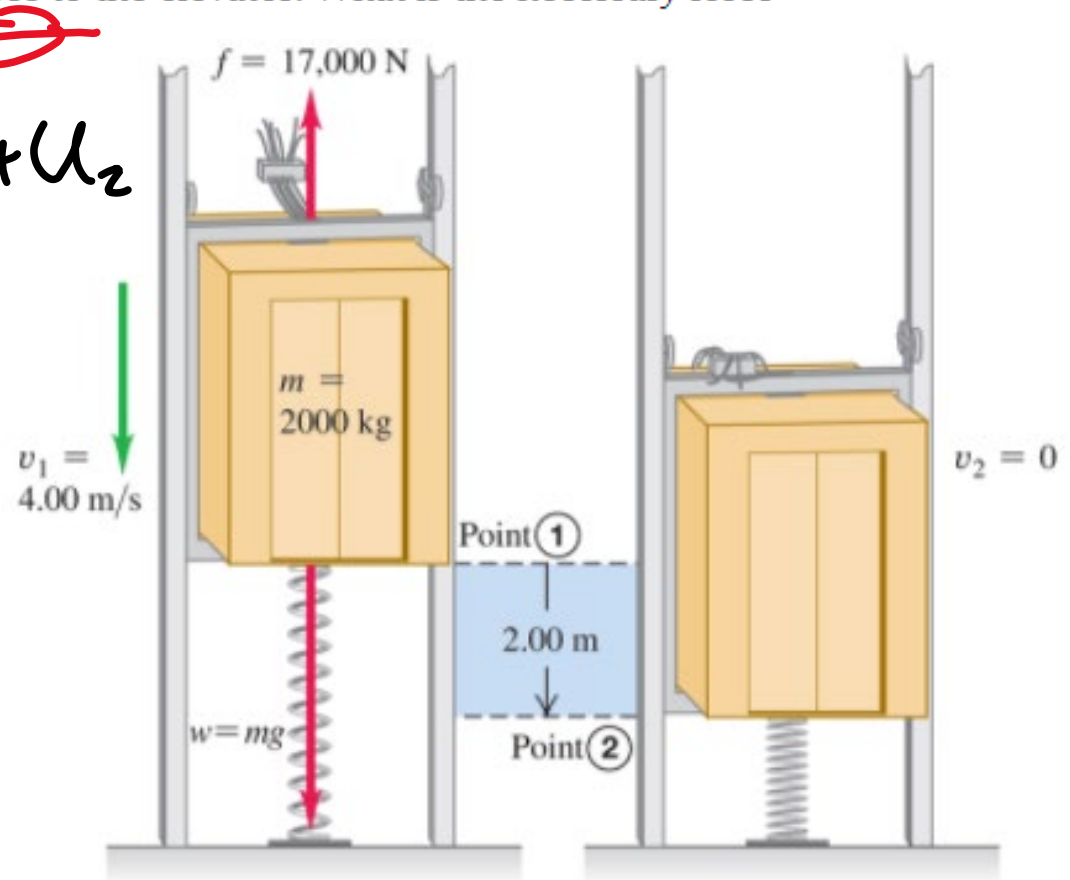


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so

$$\frac{1}{2}ky^2 = \frac{1}{2}mv_1^2 + mgy - Fy$$



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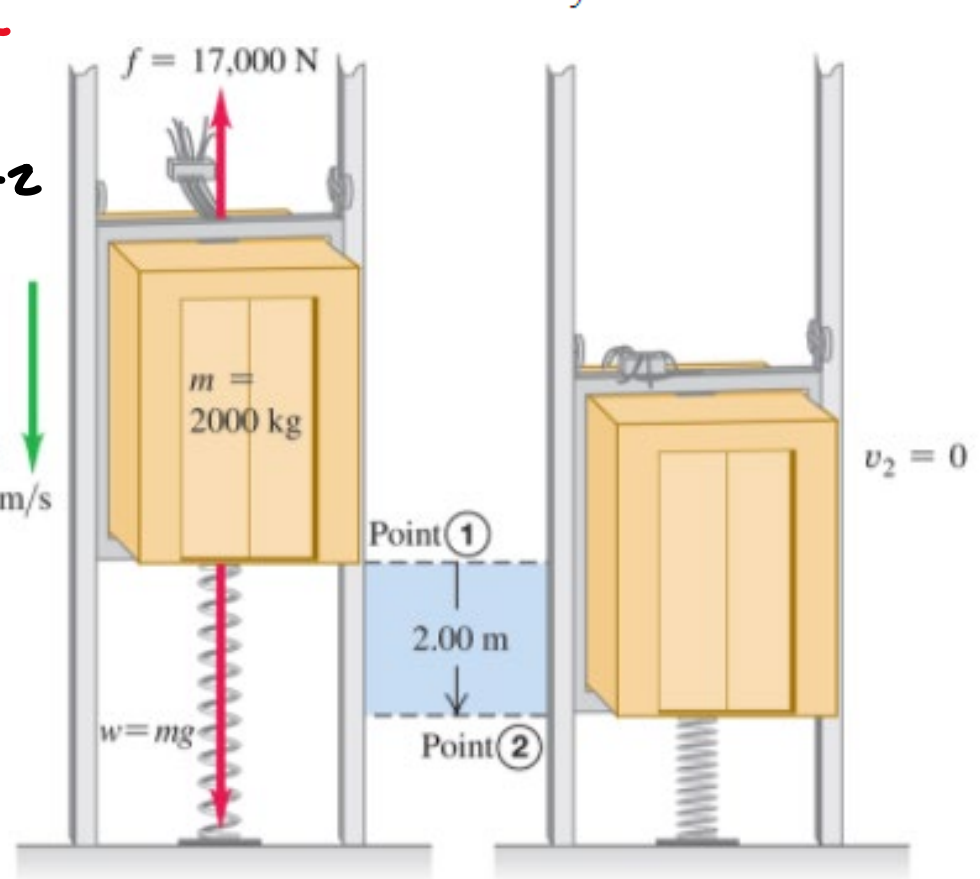
$$K_1 + U_1 + W_{\text{other}} = K_2 + U_2$$

So

$$\frac{1}{2}ky^2 = \frac{1}{2}mv_1^2 + mgy - Fy$$

⇒

$$k = \frac{m}{y^2}v_1^2 + \frac{mgy}{y} - \frac{F}{y}$$



A 2000 kg (19,600 N) elevator with broken cables in a test rig is falling at 4.00 m/s when it contacts a cushioning spring at the bottom of the shaft. The spring is intended to stop the elevator, compressing 2.00 m as it does so (Fig. 7.17). During the motion a safety clamp applies a constant 17,000 N friction force to the elevator. What is the necessary force constant  $k$  for the spring?

$$K_1 + U_1 + W_{\text{other}} = \cancel{K_2} + U_2$$

So

$$\frac{1}{2}ky^2 = \frac{1}{2}mv_i^2 + mgy - Fy$$

⇒

$$k = \frac{m}{y^2}v_i^2 + \left(\frac{mg}{y} - \frac{F}{y}\right)2$$

$$\Rightarrow k = \left[ \frac{2000}{4}16 + \left( \frac{2000 \times 9.8}{2} - \frac{17000}{2} \right)2 \right] \frac{N}{m}$$

A 2000 kg (19,600 N) elevator with broken cables in a test rig is falling at 4.00 m/s when it contacts a cushioning spring at the bottom of the shaft. The spring is intended to stop the elevator, compressing 2.00 m as it does so (Fig. 7.17). During the motion a safety clamp applies a constant 17,000 N friction force to the elevator. What is the necessary force constant  $k$  for the spring?

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⇒

$$k = \frac{m}{y^2}v_i^2 + \left(\frac{mg}{y} - \frac{F}{y}\right)2$$

$$\Rightarrow k = \left[ \frac{2000}{4} (16) + \left( \frac{2000 \times 9.8}{2} - \frac{17000}{2} \right) 2 \right] \frac{\text{N}}{\text{m}} = 10600 \text{ N/m}$$





