

Today: 4.1 & 4.2

211



Today: 4.1 & 4.2

(211)

Force's

Today: 4.1 & 4.2

211

Newton's  
1<sup>ST</sup>  
law

Today: 4.1 & 4.2

(211)

Monday: 4.3 & 4.4

Today: 4.1 & 4.2

(211)

Monday: 4.3 & 4.4

Newton's  
2<sup>nd</sup> law

Today: 4.1 & 4.2

(211)

Monday: 4.3 & 4.4

Mass &  
Weight

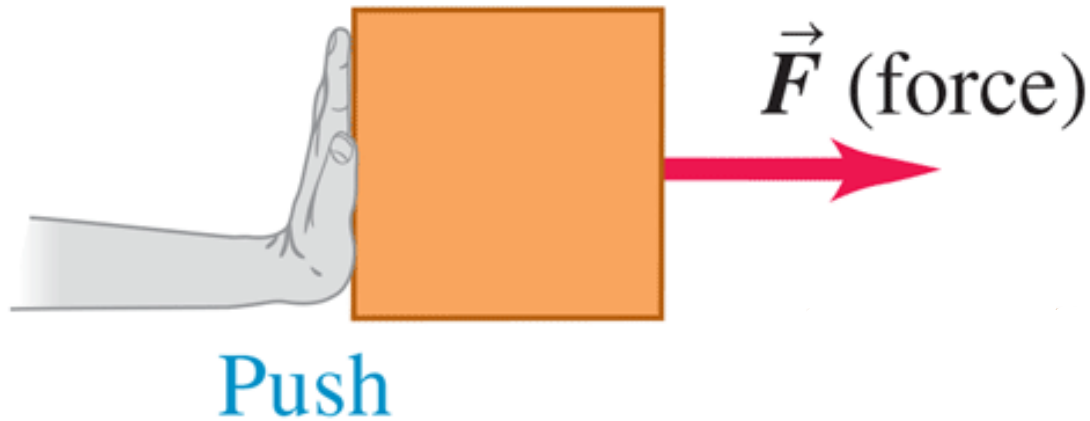
# Force & interaction

# Force & interaction

- A force is a push or a pull.

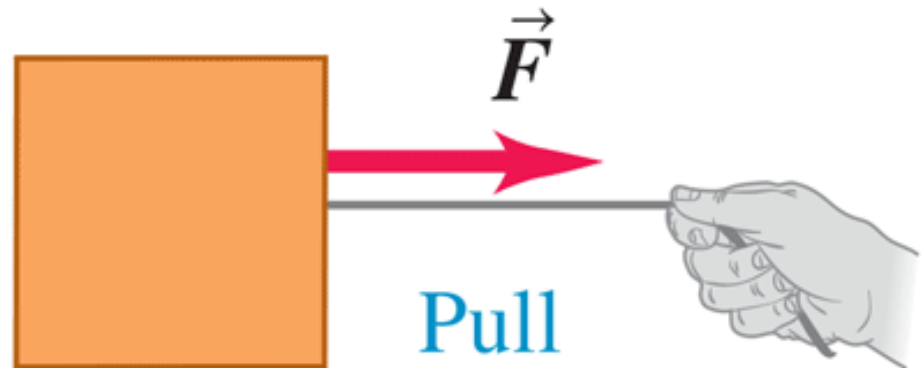
# Force & interaction

- A force is a push or a pull.



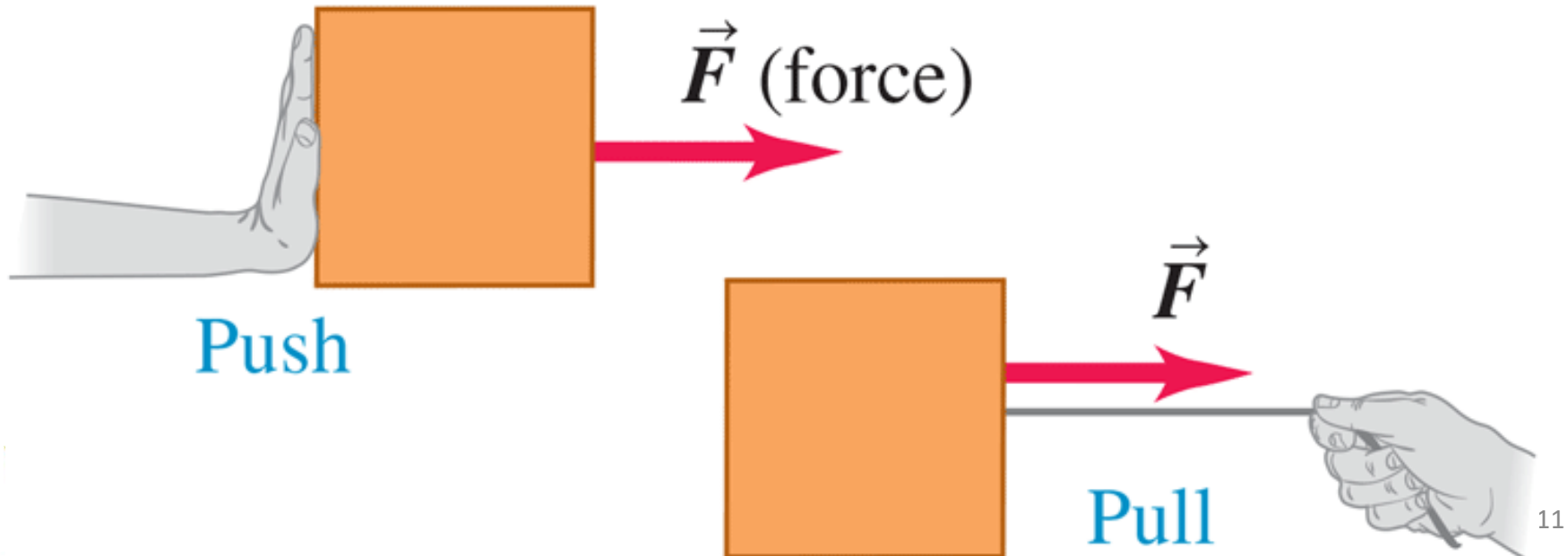
# Force & interaction

- A force is a push or a pull.



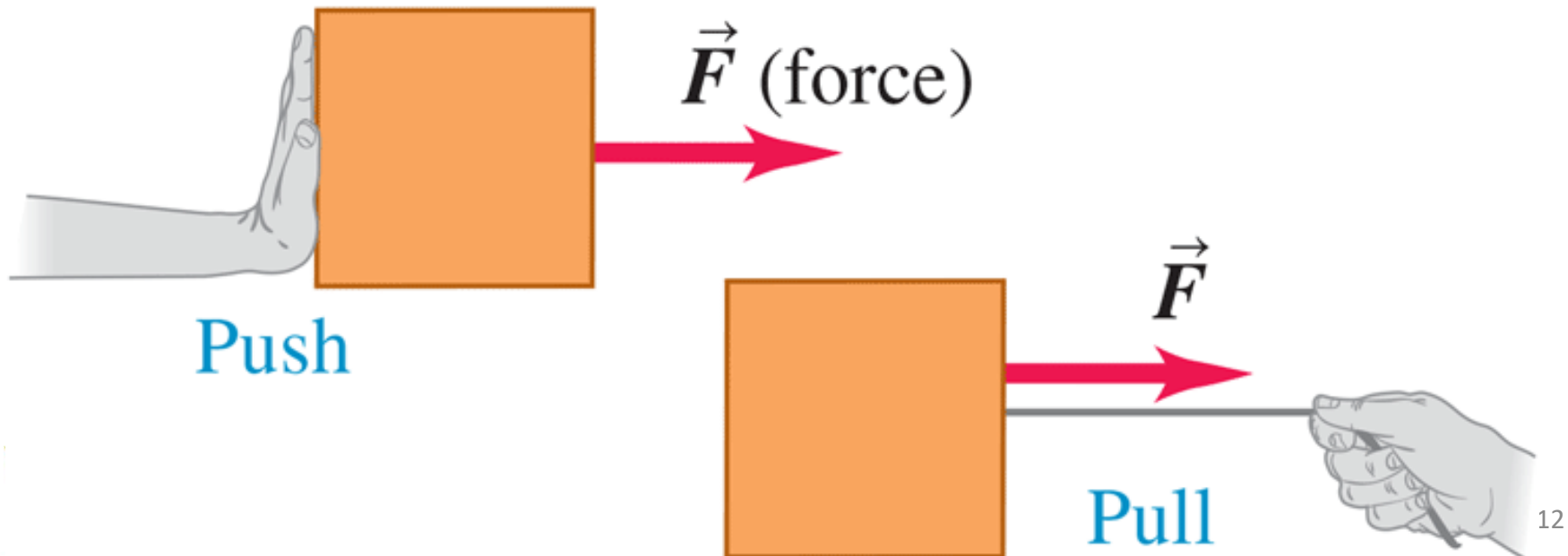
# Force & interaction

- A force is a push or a pull.
- A force is an interaction between two objects or between an object and its environment.



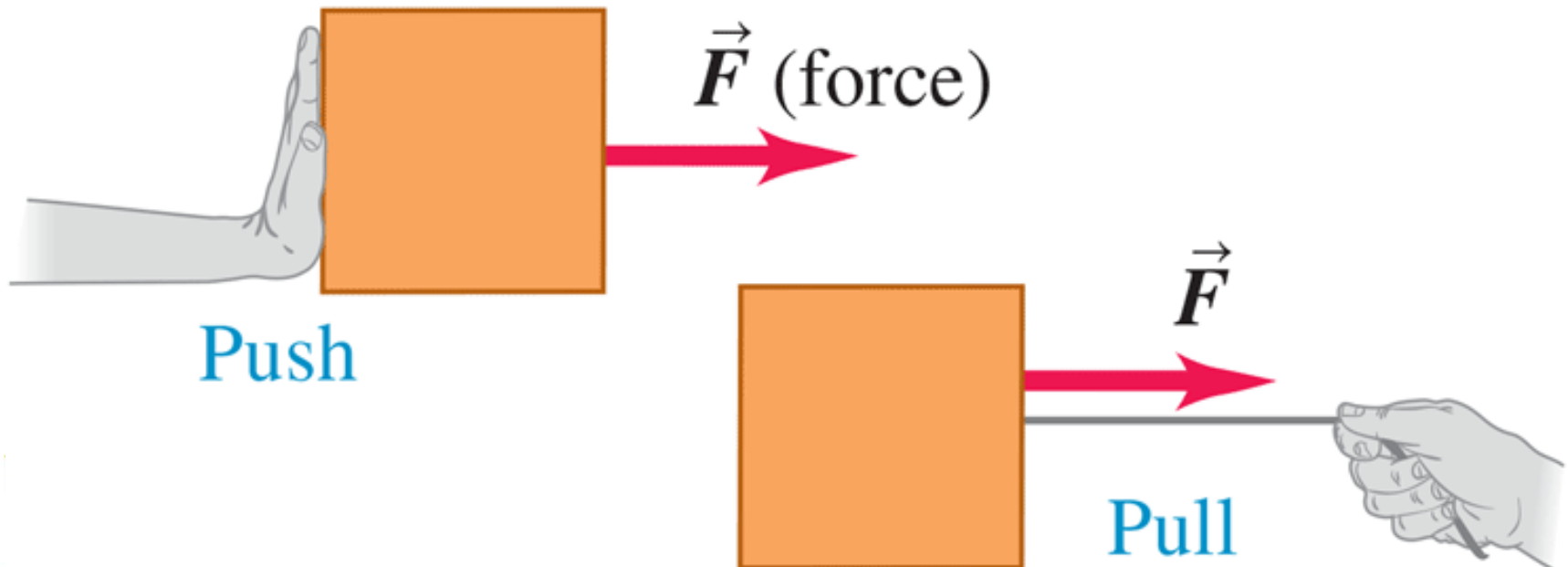
# Force & interaction

- A force is a push or a pull.
- A force is an interaction between two objects or between an object and its environment.
- A force is a vector quantity, with magnitude and direction.



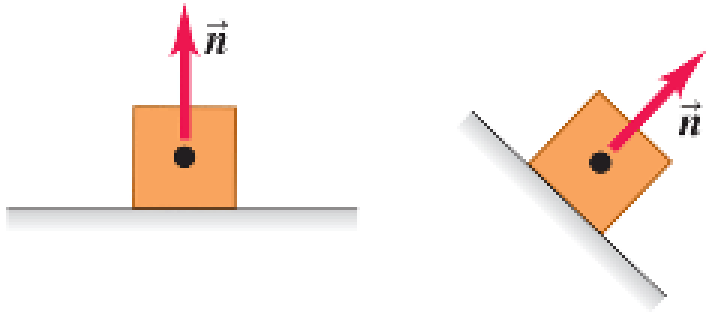
# Force & interaction

- A force is a push or a pull.
- A force is an interaction between two objects or between an object and its environment.
- A force is a vector quantity, with magnitude and direction.



# Force & interaction

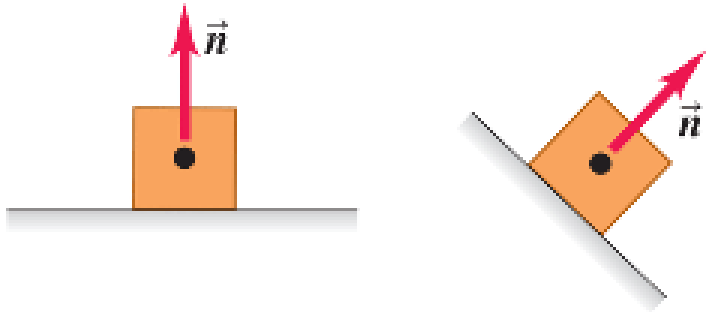
(a) **Normal force  $\vec{n}$ :** When an object rests or pushes on a surface, the surface exerts a push on it that is directed perpendicular to the surface.



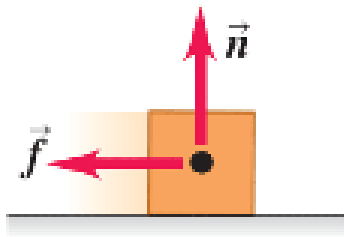
↖  
Contact  
force

# Force & interaction

(a) **Normal force  $\vec{n}$ :** When an object rests or pushes on a surface, the surface exerts a push on it that is directed perpendicular to the surface.



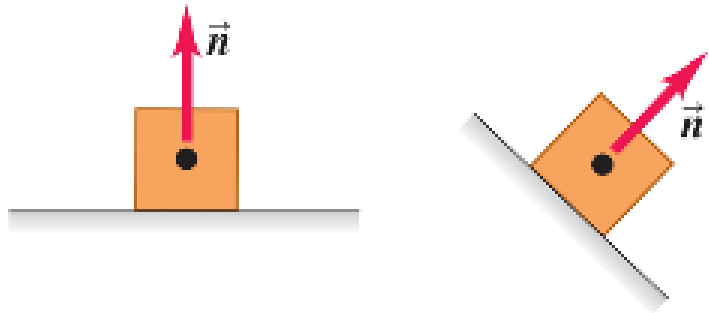
(b) **Friction force  $\vec{f}$ :** In addition to the normal force, a surface may exert a friction force on an object, directed parallel to the surface.



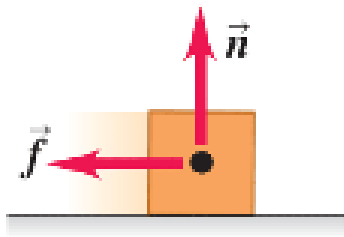
↖  
Contact  
force  
↖

# Force & interaction

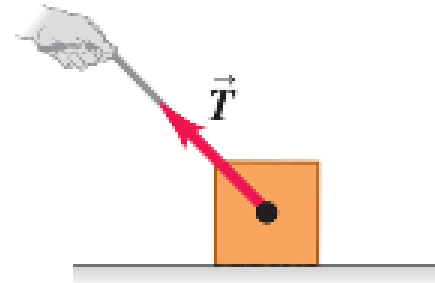
(a) **Normal force  $\vec{n}$ :** When an object rests or pushes on a surface, the surface exerts a push on it that is directed perpendicular to the surface.



(b) **Friction force  $\vec{f}$ :** In addition to the normal force, a surface may exert a friction force on an object, directed parallel to the surface.



(c) **Tension force  $\vec{T}$ :** A pulling force exerted on an object by a rope, cord, etc.

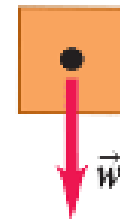


↑  
↙  
↖  
Contact  
force

# Force & interaction

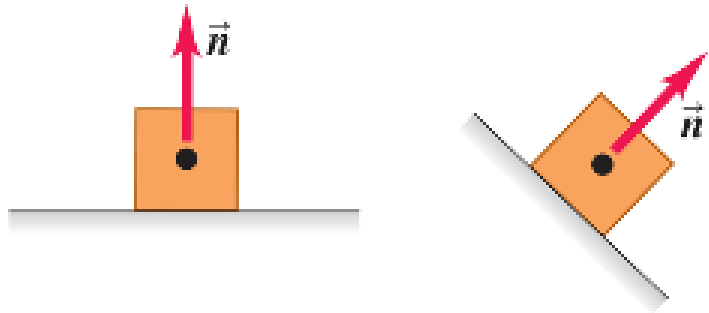
Long range  
force  
↓

(d) **Weight  $\vec{w}$** : The pull of gravity on an object is a long-range force (a force that acts over a distance).

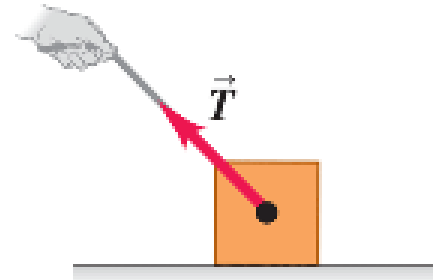


# Force & interaction

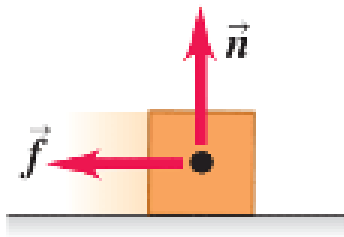
(a) **Normal force  $\vec{n}$ :** When an object rests or pushes on a surface, the surface exerts a push on it that is directed perpendicular to the surface.



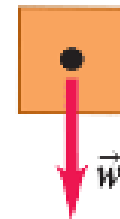
(c) **Tension force  $\vec{T}$ :** A pulling force exerted on an object by a rope, cord, etc.



(b) **Friction force  $\vec{f}$ :** In addition to the normal force, a surface may exert a friction force on an object, directed parallel to the surface.



(d) **Weight  $\vec{w}$ :** The pull of gravity on an object is a long-range force (a force that acts over a distance).



# Force & interaction

Let

$\vec{F} \equiv$  force vector

# Force & interaction

Let

$\vec{F} \equiv$  force vector

---

Units of force:

# Force & interaction

Let

$\vec{F} \equiv$  force vector

---

Units of force:  $N \equiv$  Newton (SI)

# Force & interaction

Let

$\vec{F} \equiv$  force vector

---

Units of force:  $N \equiv$  Newton (SI)

Pound  $\equiv$  lb (US)

# Force & interaction

Let

$\vec{F} \equiv$  force vector

---

Units of force:  $N \equiv$  Newton (SI)

Pound  $\equiv$  lb (US)

Also Force =

# Force & interaction

Let

$\vec{F} \equiv$  force vector

---

Units of force:  $N \equiv$  Newton (SI)

Pound  $\equiv$  lb (US)

Also  $\text{Force} = (\text{mass}) \cdot$

# Force & interaction

Let

$\vec{F} \equiv$  force vector

---

Units of force:  $N \equiv$  Newton (SI)

Pound  $\equiv$  lb (US)

Also  $\text{Force} = \underline{(\text{mass}) * (\text{distance})}$

# Force & interaction

Let

$\vec{F} \equiv$  force vector

---

Units of force:  $N \equiv$  Newton (SI)

Pound  $\equiv$  lb (US)

$$\text{Also } \text{Force} = \frac{(\text{mass}) * (\text{distance})}{(\text{time})^2}$$

# Force & interaction

Table 4.1 Typical Force Magnitudes

Sun's gravitational force on the earth	$3.5 \times 10^{22} \text{ N}$
Weight of a large blue whale	$1.9 \times 10^6 \text{ N}$
Maximum pulling force of a locomotive	$8.9 \times 10^5 \text{ N}$
Weight of a 250 lb linebacker	$1.1 \times 10^3 \text{ N}$
Weight of a medium apple	1 N
Weight of the smallest insect eggs	$2 \times 10^{-6} \text{ N}$
Electric attraction between the proton and the electron in a hydrogen atom	$8.2 \times 10^{-8} \text{ N}$
Weight of a very small bacterium	$1 \times 10^{-18} \text{ N}$
Weight of a hydrogen atom	$1.6 \times 10^{-26} \text{ N}$
Weight of an electron	$8.9 \times 10^{-30} \text{ N}$
Gravitational attraction between the proton and the electron in a hydrogen atom	$3.6 \times 10^{-47} \text{ N}$

# Force & interaction

Table 4.1 Typical Force Magnitudes

Sun's gravitational force on the earth	$3.5 \times 10^{22} \text{ N}$
Weight of a large blue whale	$1.9 \times 10^6 \text{ N}$
Maximum pulling force of a locomotive	$8.9 \times 10^5 \text{ N}$
Weight of a 250 lb linebacker	$1.1 \times 10^3 \text{ N}$
Weight of a medium apple	1 N
Weight of the smallest insect eggs	$2 \times 10^{-6} \text{ N}$
Electric attraction between the proton and the electron in a hydrogen atom	$8.2 \times 10^{-8} \text{ N}$
Weight of a very small bacterium	$1 \times 10^{-18} \text{ N}$
Weight of a hydrogen atom	$1.6 \times 10^{-26} \text{ N}$
Weight of an electron	$8.9 \times 10^{-30} \text{ N}$
Gravitational attraction between the proton and the electron in a hydrogen atom	$3.6 \times 10^{-47} \text{ N}$

# Force & interaction

Table 4.1 Typical Force Magnitudes

Sun's gravitational force on the earth	$3.5 \times 10^{22} \text{ N}$
Weight of a large blue whale	$1.9 \times 10^6 \text{ N}$
Maximum pulling force of a locomotive	$8.9 \times 10^5 \text{ N}$
Weight of a 250 lb linebacker	$1.1 \times 10^3 \text{ N}$
Weight of a medium apple	1 N
Weight of the smallest insect eggs	$2 \times 10^{-6} \text{ N}$
Electric attraction between the proton and the electron in a hydrogen atom	$8.2 \times 10^{-8} \text{ N}$
Weight of a very small bacterium	$1 \times 10^{-18} \text{ N}$
Weight of a hydrogen atom	$1.6 \times 10^{-26} \text{ N}$
Weight of an electron	$8.9 \times 10^{-30} \text{ N}$
Gravitational attraction between the proton and the electron in a hydrogen atom	$3.6 \times 10^{-47} \text{ N}$

Also  
 $1 \text{ lb} = 4.45 \text{ N}$



# Force & interaction

Table 4.1 Typical Force Magnitudes

Sun's gravitational force on the earth	$3.5 \times 10^{22} \text{ N}$
Weight of a large blue whale	$1.9 \times 10^6 \text{ N}$
Maximum pulling force of a locomotive	$8.9 \times 10^5 \text{ N}$
Weight of a 250 lb linebacker	$1.1 \times 10^3 \text{ N}$
Weight of a medium apple	1 N
Weight of the smallest insect eggs	$2 \times 10^{-6} \text{ N}$
Electric attraction between the proton and the electron in a hydrogen atom	$8.2 \times 10^{-8} \text{ N}$
Weight of a very small bacterium	$1 \times 10^{-18} \text{ N}$
Weight of a hydrogen atom	$1.6 \times 10^{-26} \text{ N}$
Weight of an electron	$8.9 \times 10^{-30} \text{ N}$
Gravitational attraction between the proton and the electron in a hydrogen atom	$3.6 \times 10^{-47} \text{ N}$

Also  
 $1 \text{ lb} = 4.45 \text{ N}$       or       $1 \text{ N} = 0.225 \text{ lb}$



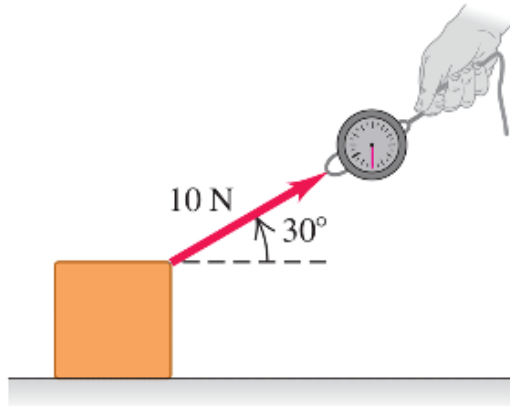
Force & interaction

Force is a vector

# Force & interaction

## Force is a vector

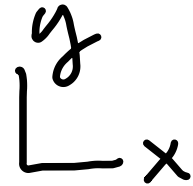
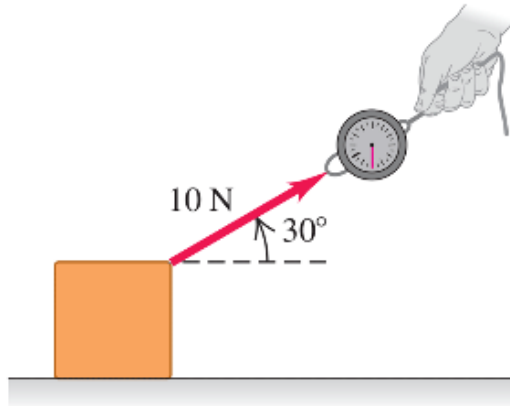
(a) A 10 N pull directed  $30^\circ$  above the horizontal



# Force & interaction

## Force is a vector

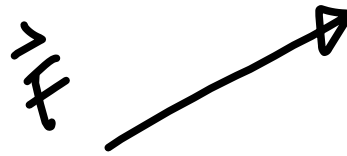
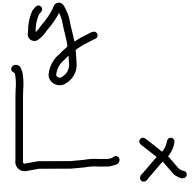
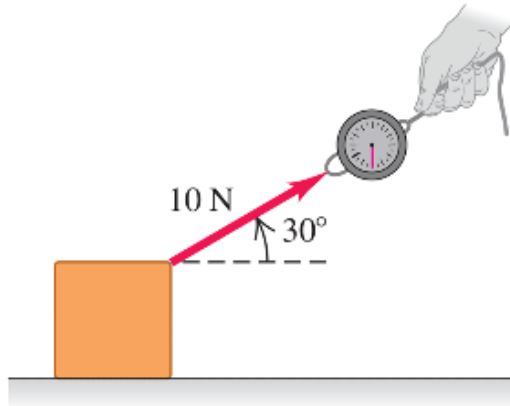
(a) A 10 N pull directed  $30^\circ$  above the horizontal



# Force & interaction

## Force is a vector

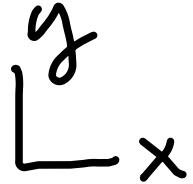
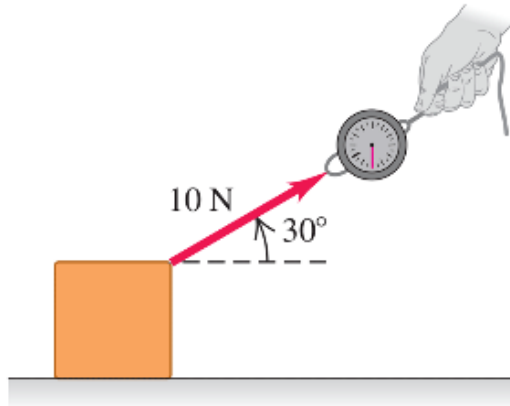
(a) A 10 N pull directed  $30^\circ$  above the horizontal



# Force & interaction

## Force is a vector

(a) A 10 N pull directed  $30^\circ$  above the horizontal



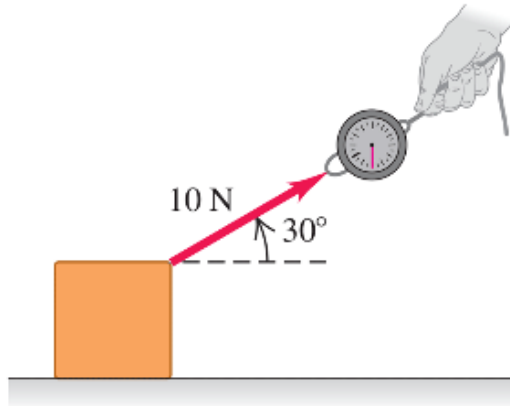
$$\vec{F} = F \cos 30^\circ \hat{x}$$

$F(\cos 30^\circ) \hat{x}$

# Force & interaction

## Force is a vector

(a) A 10 N pull directed  $30^\circ$  above the horizontal



$\vec{F} = F_x \hat{i} + F_y \hat{j}$

$F(\cos 30^\circ) \hat{i}$

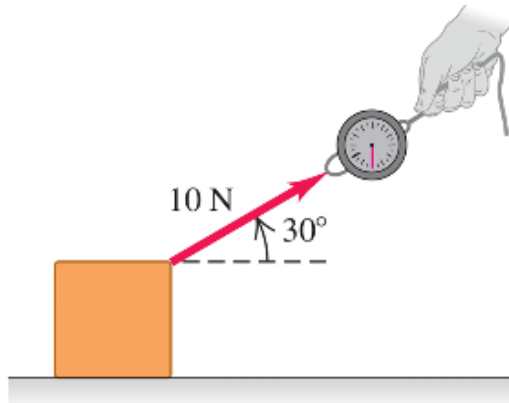
$F(\sin 30^\circ) \hat{j}$

A hand-drawn diagram showing a right-angled triangle representing the decomposition of a force vector. The hypotenuse is the force vector  $\vec{F}$ . The horizontal base is labeled  $F(\cos 30^\circ) \hat{i}$  and the vertical height is labeled  $F(\sin 30^\circ) \hat{j}$ . A coordinate system with  $x$  and  $y$  axes is shown in the upper right. The equation  $\vec{F} = F_x \hat{i} + F_y \hat{j}$  is written above the triangle, with  $F_x \hat{i} + F_y \hat{j}$  circled in yellow.

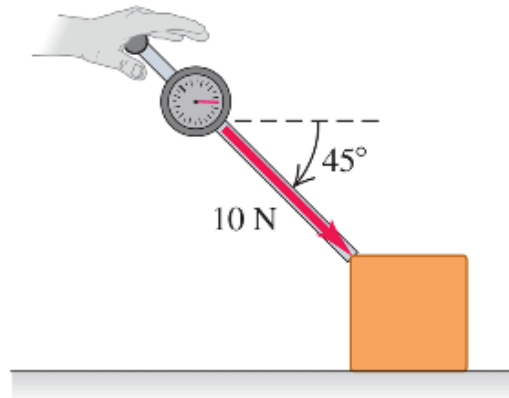
# Force & interaction

## Force is a vector

(a) A 10 N pull directed  $30^\circ$  above the horizontal



(b) A 10 N push directed  $45^\circ$  below the horizontal



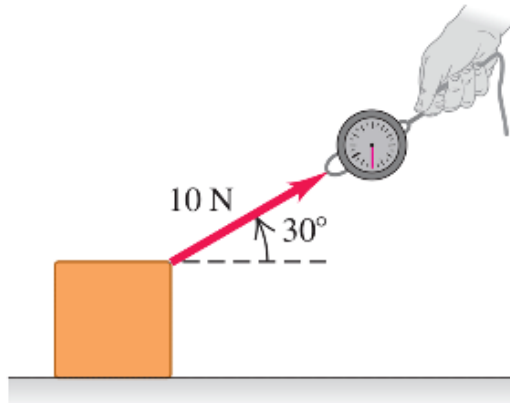
A hand-drawn diagram showing a force vector  $\vec{F}$  being decomposed into its components. The vector is shown as the hypotenuse of a right-angled triangle. The horizontal component is labeled  $F(\cos 30^\circ)\hat{i}$  and the vertical component is labeled  $F(\sin 30^\circ)\hat{j}$ . Above the diagram, the vector equation is written as  $\vec{F} = F_x\hat{i} + F_y\hat{j}$ . To the right, a small coordinate system is shown with a vertical y-axis and a horizontal x-axis.

$$\vec{F} = F_x\hat{i} + F_y\hat{j}$$
$$F(\cos 30^\circ)\hat{i}$$
$$F(\sin 30^\circ)\hat{j}$$

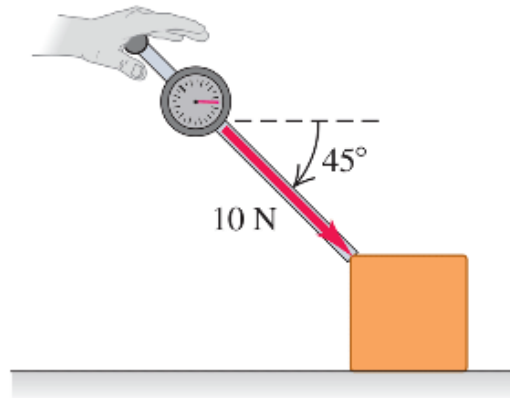
# Force & interaction

## Force is a vector

(a) A 10 N pull directed  $30^\circ$  above the horizontal



(b) A 10 N push directed  $45^\circ$  below the horizontal

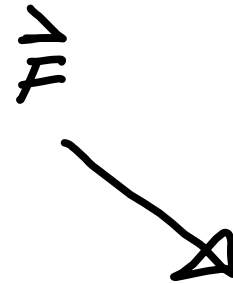


$\vec{F} = F_x \hat{i} + F_y \hat{j}$

$F(\cos 30^\circ) \hat{i}$

$F(\sin 30^\circ) \hat{j}$

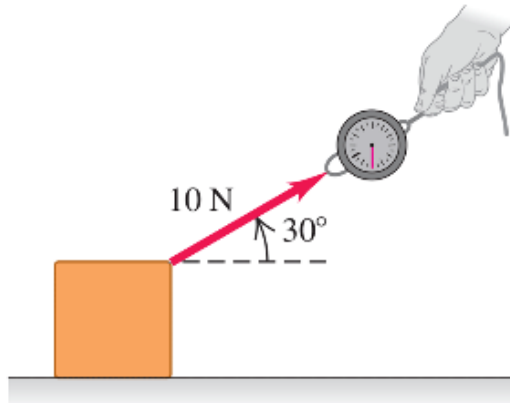
A hand-drawn vector diagram illustrating the decomposition of a force vector  $\vec{F}$  into its horizontal and vertical components. The vector  $\vec{F}$  is shown as the hypotenuse of a right-angled triangle. The horizontal component is labeled  $F(\cos 30^\circ) \hat{i}$  and the vertical component is labeled  $F(\sin 30^\circ) \hat{j}$ . Above the diagram, a coordinate system is drawn with a vertical  $y$ -axis and a horizontal  $x$ -axis.



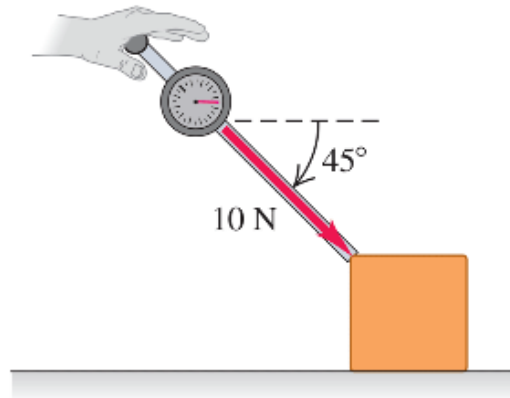
# Force & interaction

## Force is a vector

(a) A 10 N pull directed 30° above the horizontal



(b) A 10 N push directed 45° below the horizontal



$\vec{F} = F_x \hat{i} + F_y \hat{j}$

$F(\cos 30^\circ) \hat{i}$

$F(\sin 30^\circ) \hat{j}$

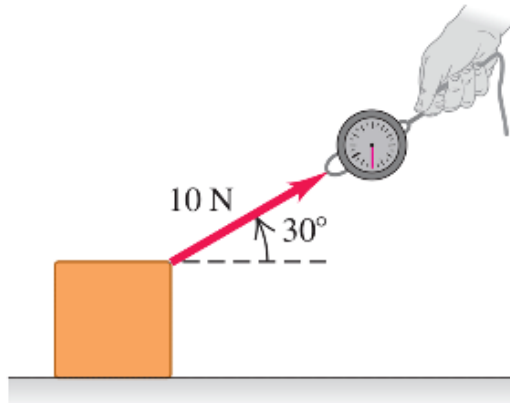
$\vec{F} = F_x \hat{i} +$

$F(\cos \theta) \hat{i}$

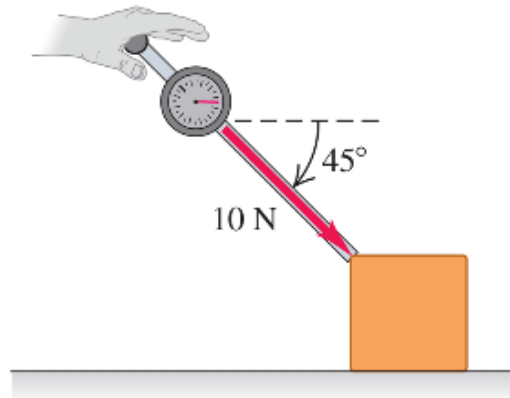
# Force & interaction

## Force is a vector

(a) A 10 N pull directed  $30^\circ$  above the horizontal



(b) A 10 N push directed  $45^\circ$  below the horizontal



$\vec{F} = F_x \hat{i} + F_y \hat{j}$

A hand-drawn vector diagram showing a force vector  $\vec{F}$  at an angle of  $30^\circ$  above the horizontal  $\hat{i}$  axis. The horizontal component is labeled  $F(\cos 30^\circ) \hat{i}$  and the vertical component is labeled  $F(\sin 30^\circ) \hat{j}$ . A coordinate system with  $x$  and  $y$  axes is shown in the upper right.

$F(\cos 30^\circ) \hat{i}$

$F(\sin 30^\circ) \hat{j}$

$\vec{F} = F_x \hat{i} + F_y \hat{j}$

A hand-drawn vector diagram showing a force vector  $\vec{F}$  at an angle of  $45^\circ$  below the horizontal  $\hat{i}$  axis. The horizontal component is labeled  $F(\cos \theta) \hat{i}$  and the vertical component is labeled  $F(\sin \theta) \hat{j}$ .

$F(\sin \theta) \hat{j}$

$F(\cos \theta) \hat{i}$

# Superposition

# Superposition

Any number of forces applied at a point on an object have the same effect as a single force equal to the vector sum of the forces

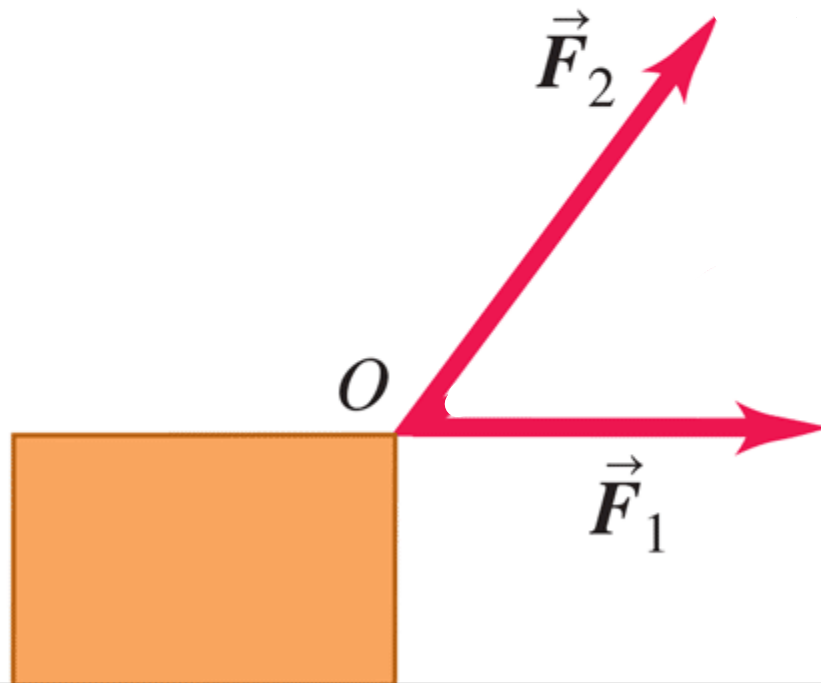
# Superposition

Any number of forces applied at a point on an object have the same effect as a single force equal to the vector sum of the forces

Superposition  
of  
Forces

# Superposition

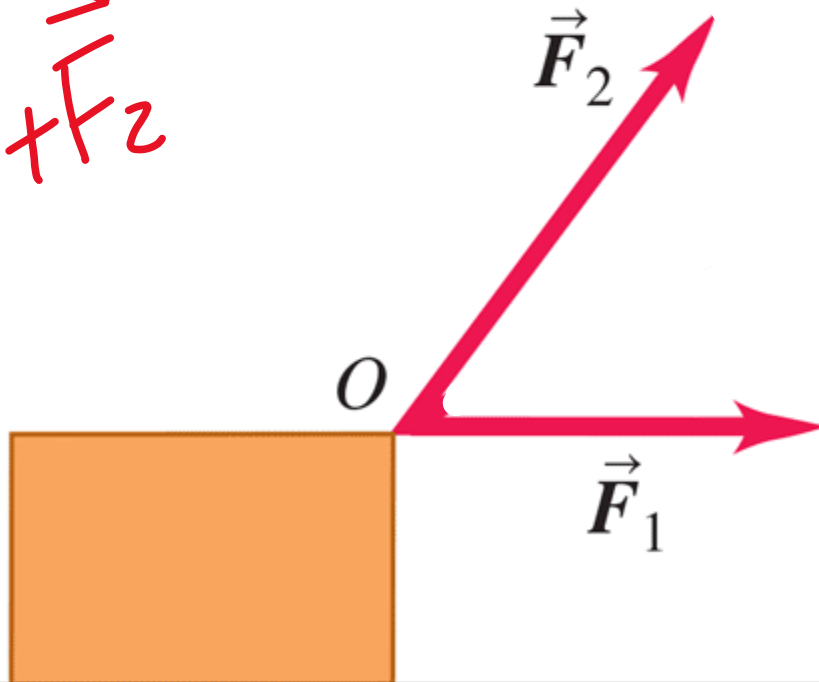
Two forces  $\vec{F}_1$  and  $\vec{F}_2$  acting on an object at point  $O$



# Superposition

Two forces  $\vec{F}_1$  and  $\vec{F}_2$  acting on an object at point  $O$

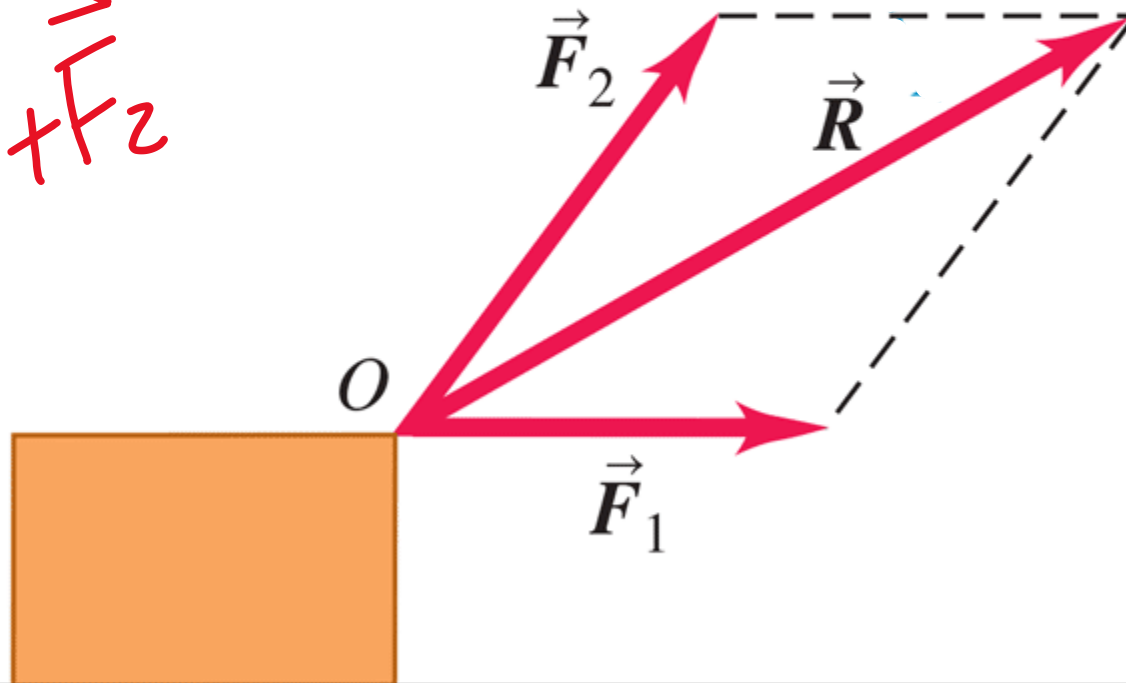
Let  
 $\vec{R} = \vec{F}_1 + \vec{F}_2$



# Superposition

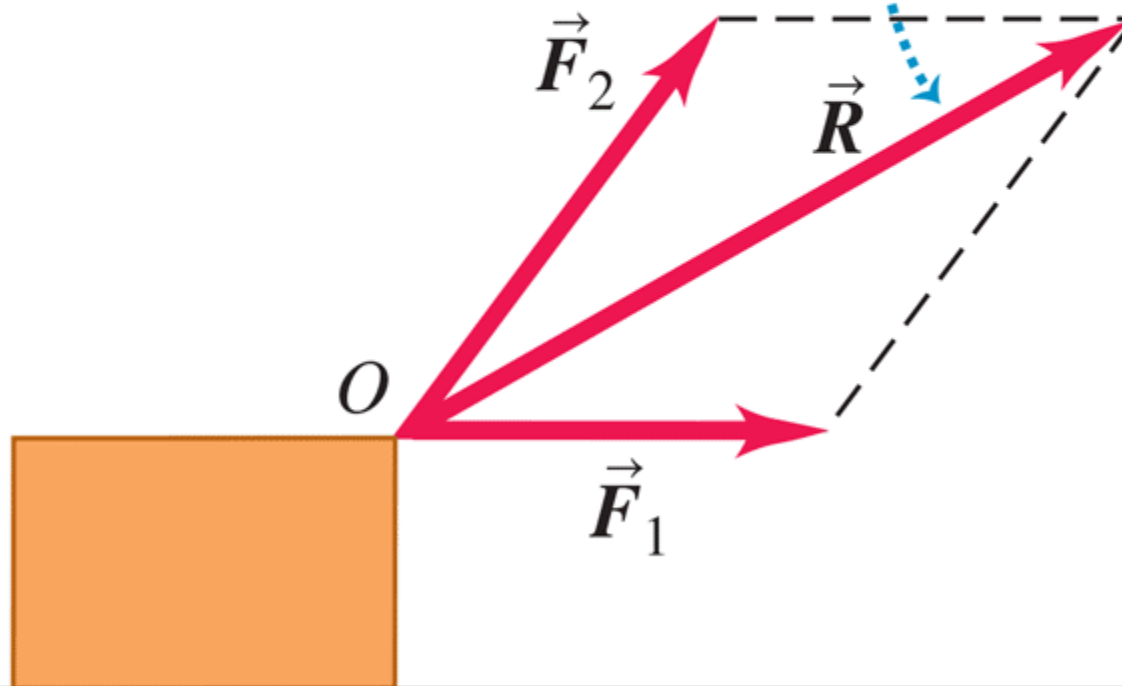
Two forces  $\vec{F}_1$  and  $\vec{F}_2$  acting on an object at point  $O$

Let  
$$\vec{R} = \vec{F}_1 + \vec{F}_2$$



# Superposition

Two forces  $\vec{F}_1$  and  $\vec{F}_2$  acting on an object at point  $O$  have the same effect as a single force  $\vec{R}$  equal to their vector sum.



# Superposition

Notation:  $\Sigma \equiv \text{SUM}$

# Superposition

Notation:  $\Sigma \equiv \text{sum}$

Now  $\vec{R} = \Sigma \vec{F}$

# Superposition

Notation:

$\Sigma \equiv \text{sum}$

Now  $\vec{R} = \Sigma \vec{F} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \dots$

# Superposition

Notation:  $\Sigma \equiv \text{sum}$

Now  $\vec{R} = \Sigma \vec{F} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \dots$

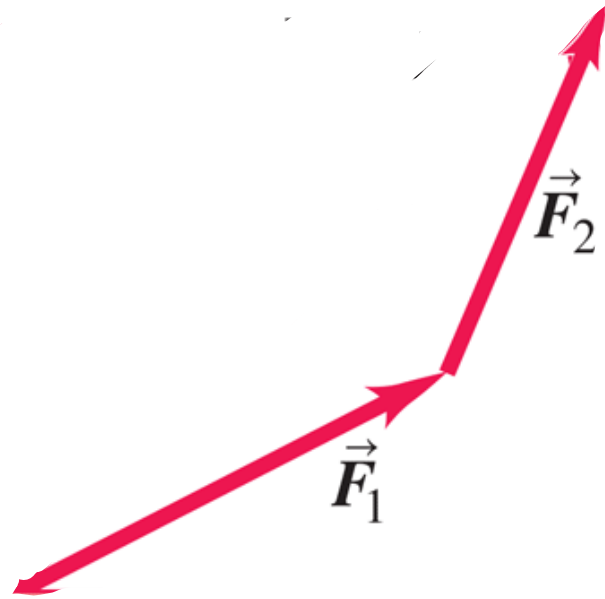
$$\Rightarrow R_x = \Sigma F_x$$

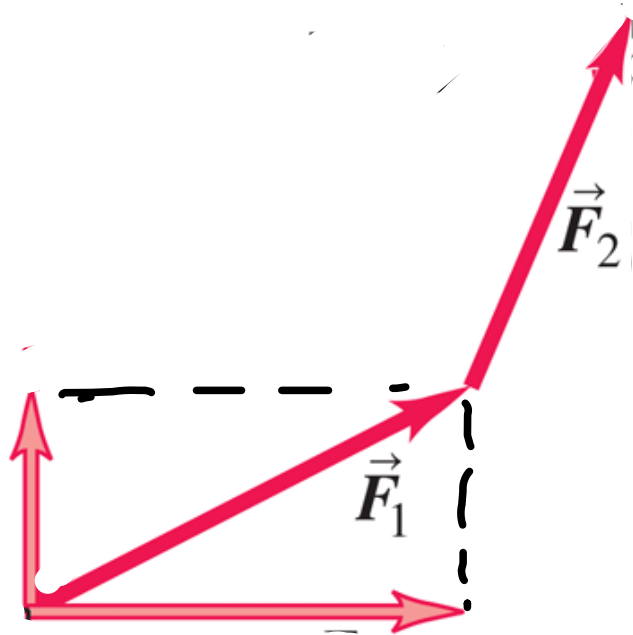
# Superposition

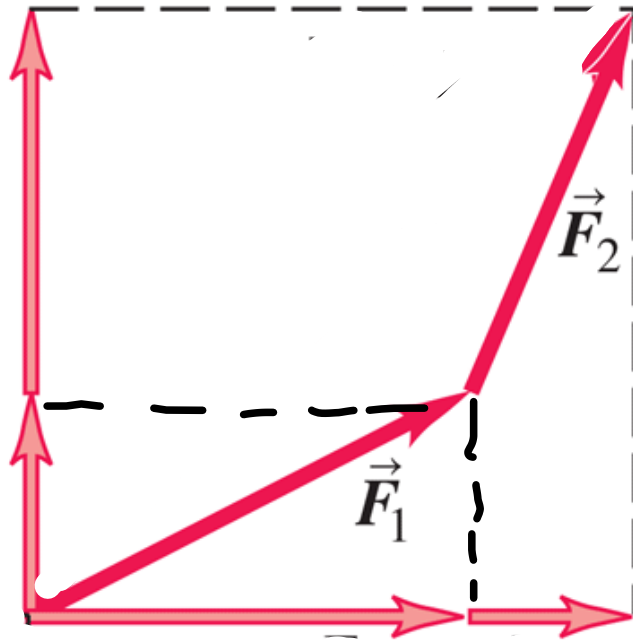
Notation:  $\Sigma \equiv \text{sum}$

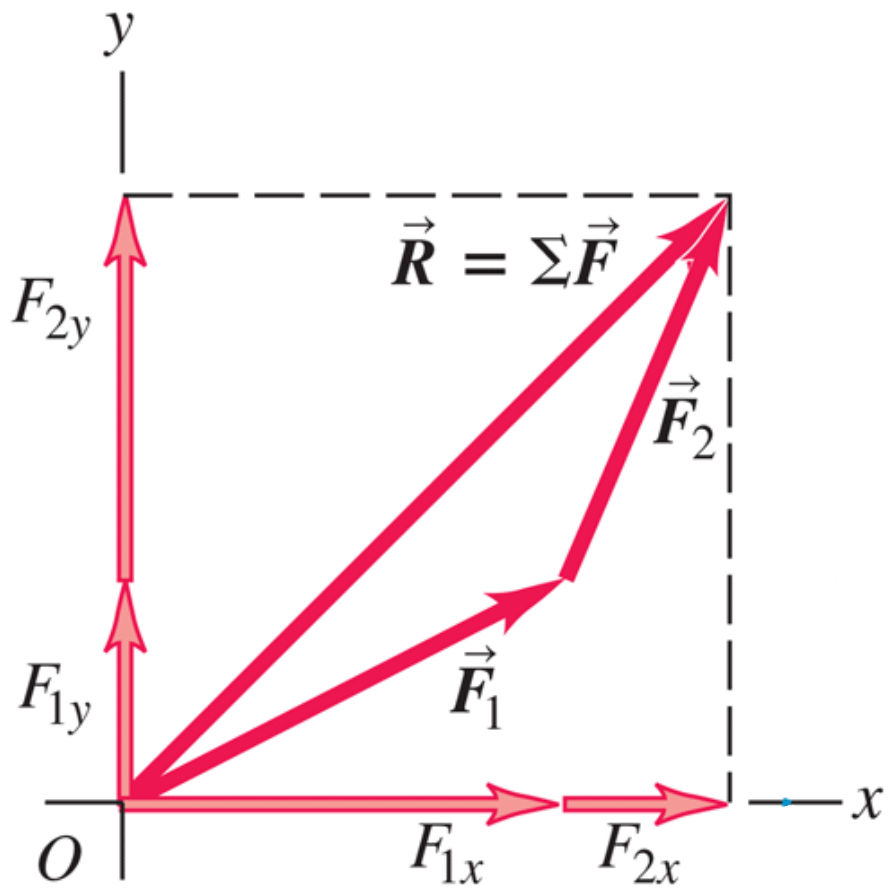
Now  $\vec{R} = \Sigma \vec{F} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \dots$

$$\Rightarrow R_x = \Sigma F_x \quad \& \quad R_y = \Sigma F_y$$

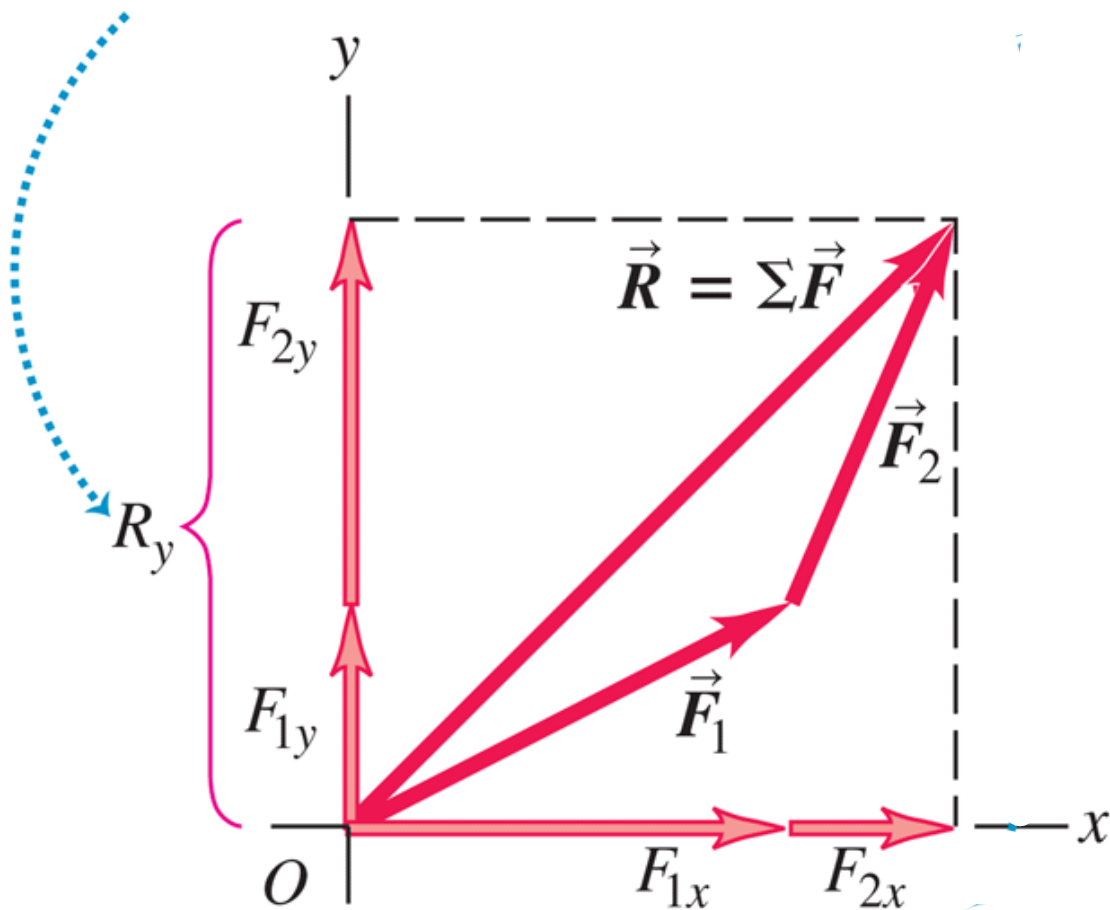






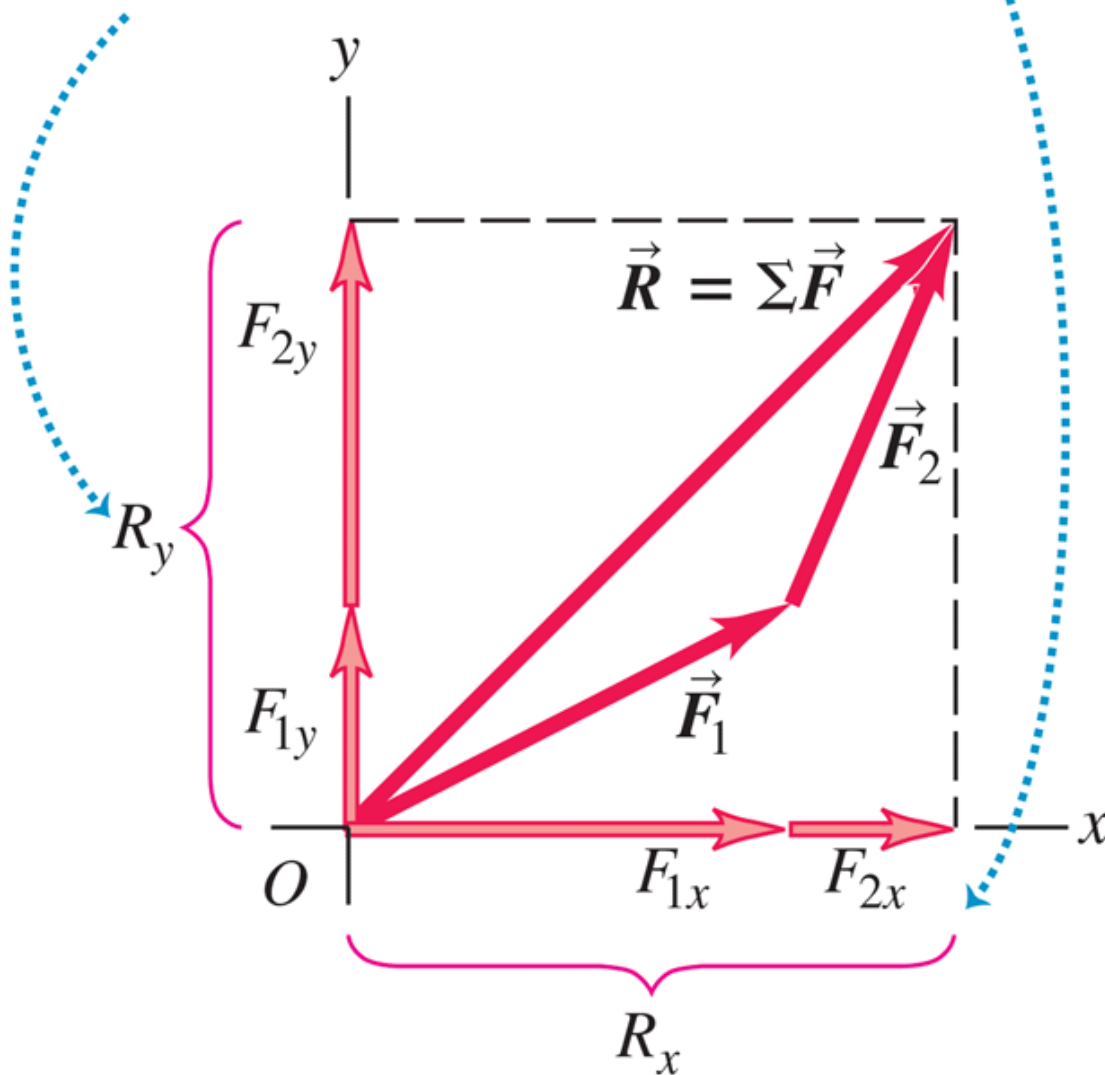


The y-component of  $\vec{R}$  equals the sum of the y-components of  $\vec{F}_1$  and  $\vec{F}_2$ .



The y-component of  $\vec{R}$  equals the sum of the y-components of  $\vec{F}_1$  and  $\vec{F}_2$ .

The same is true for the x-components.



# Superposition

Once we have  $R_x$  &  $R_y$   
we can find  $R$

# Superposition

Once we have  $R_x$  &  $R_y$   
we can find  $R$ :

$$R = [R_x^2 + R_y^2]^{1/2}$$

# Superposition

Once we have  $R_x$  &  $R_y$   
we can find  $R$ :

$$R = [R_x^2 + R_y^2]^{1/2}$$

In 3D:

# Superposition

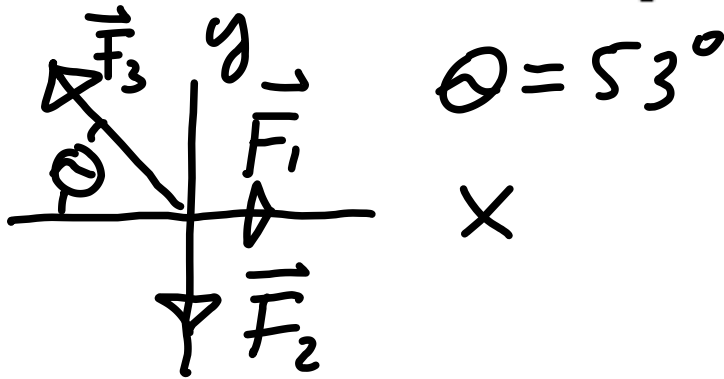
Once we have  $R_x$  &  $R_y$   
we can find  $R$ :

$$R = [R_x^2 + R_y^2]^{1/2}$$

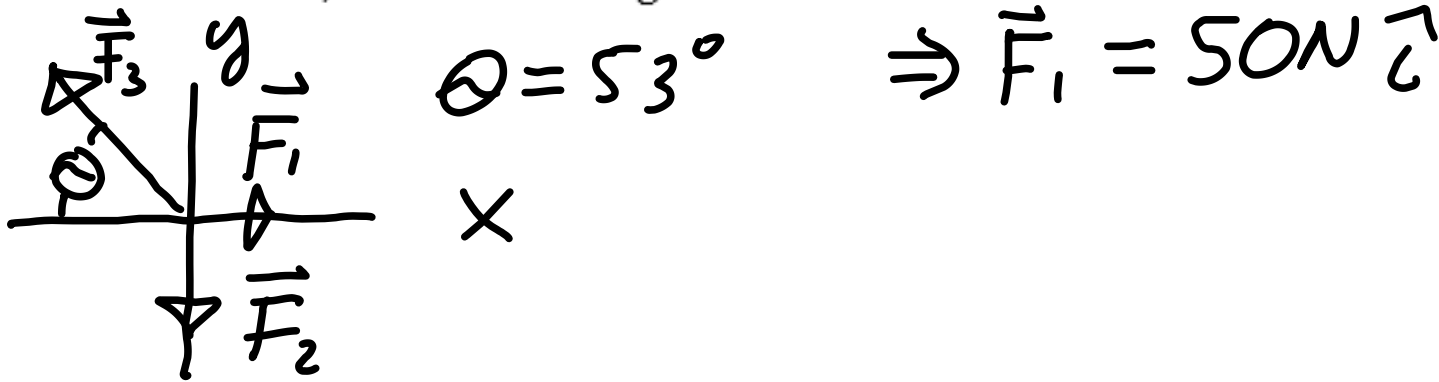
In 3D:

$$R = [R_x^2 + R_y^2 + R_z^2]^{1/2}$$

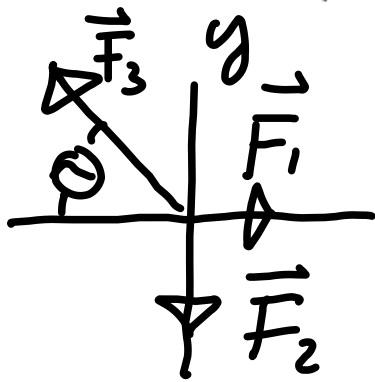
Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50$  N,  $F_2 = 120$  N, and  $F_3 = 250$  N. Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50$  N,  $F_2 = 120$  N, and  $F_3 = 250$  N. Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



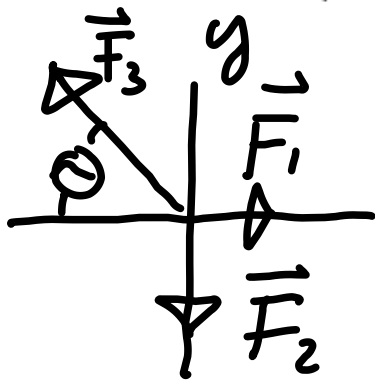
$$\theta = 53^\circ$$

x

$$\Rightarrow \vec{F}_1 = 50\text{N} \hat{j}$$

$$\& \vec{F}_2 = 120\text{N} (-\hat{j})$$

Three professional wrestlers are fighting over a champion's belt. **Figure 4.7a** shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\theta = 53^\circ$$

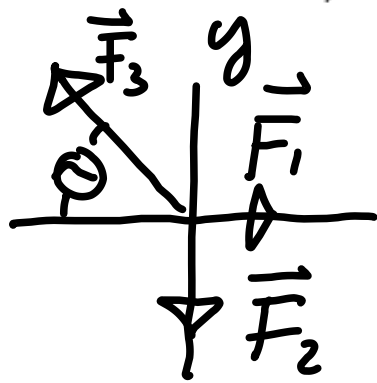
x

$$\Rightarrow \vec{F}_1 = 50 \text{ N } \hat{j}$$

$$\& \vec{F}_2 = 120 \text{ N } (-\hat{j})$$

$$\& \vec{F}_3 = F_{3x} \hat{i} + F_{3y} \hat{j}$$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50$  N,  $F_2 = 120$  N, and  $F_3 = 250$  N. Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\theta = 53^\circ$$

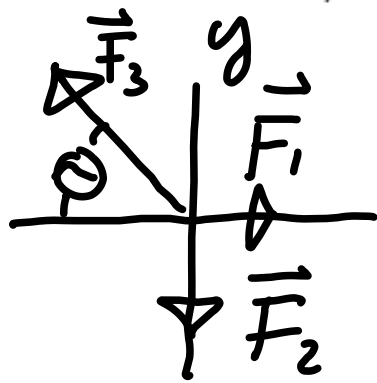
$$\Rightarrow \vec{F}_1 = 50\text{N} \hat{j}$$

$$\& \vec{F}_2 = 120\text{N} (-\hat{j})$$

$$\& \vec{F}_3 = F_{3x} \hat{i} + F_{3y} \hat{j}$$

where  $F_{3x} = 250 \text{ N} \cos(53^\circ) = 150 \text{ N}$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\theta = 53^\circ$$

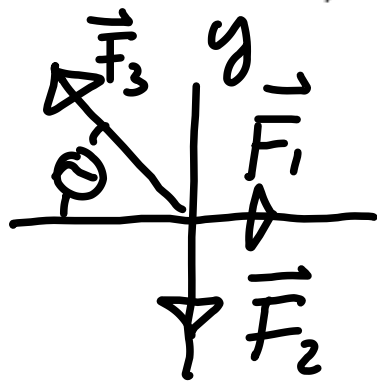
$$\Rightarrow \vec{F}_1 = 50 \text{ N } \hat{j}$$

$$\& \vec{F}_2 = 120 \text{ N } (-\hat{j})$$

$$\& \vec{F}_3 = F_{3x} \hat{i} + F_{3y} \hat{j}$$

where  $F_{3x} = 250 \text{ N } \cos(53^\circ) = 150 \text{ N}$  &  
 $F_{3y} = -250 \text{ N } \sin(53^\circ) = -200 \text{ N}$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\theta = 53^\circ$$

$$\Rightarrow \vec{F}_1 = 50\text{N} \hat{j}$$

$$\& \vec{F}_2 = 120\text{N}(-\hat{j})$$

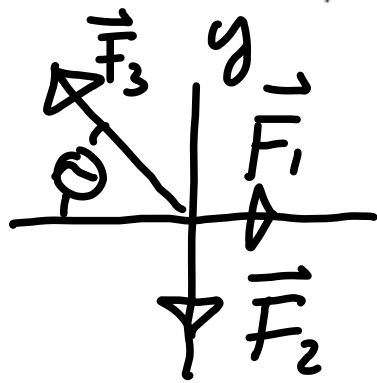
$$\& \vec{F}_3 = F_{3x} \hat{i} + F_{3y} \hat{j}$$

where  $F_{3x} = 250 \text{ N} \cos(53^\circ) = 150 \text{ N}$  &

$$F_{3y} = -250 \text{ N} \sin(53^\circ) = -200 \text{ N}$$

so  $R_x = 50 \text{ N}$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\theta = 53^\circ$$

$$\Rightarrow \vec{F}_1 = 50 \text{ N } \hat{j}$$

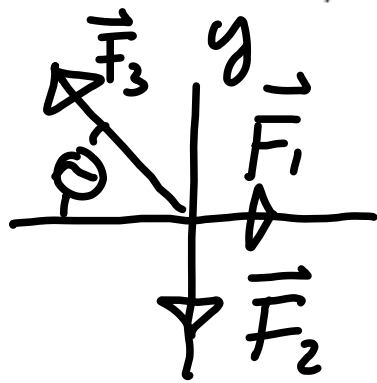
$$\& \vec{F}_2 = 120 \text{ N } (-\hat{j})$$

$$\& \vec{F}_3 = F_{3x} \hat{i} + F_{3y} \hat{j}$$

where  $F_{3x} = 250 \text{ N } \cos(53^\circ) = 150 \text{ N}$  &  
 $F_{3y} = -250 \text{ N } \sin(53^\circ) = -200 \text{ N}$

so  $R_x = 50 \text{ N} - 150 \text{ N}$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\theta = 53^\circ$$

$$\Rightarrow \vec{F}_1 = 50 \text{ N } \hat{j}$$

$$\& \vec{F}_2 = 120 \text{ N } (-\hat{j})$$

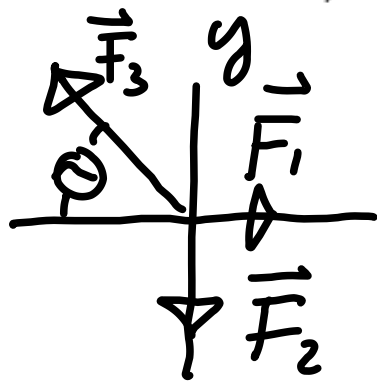
$$\& \vec{F}_3 = F_{3x} \hat{i} + F_{3y} \hat{j}$$

where  $F_{3x} = 250 \text{ N } \cos(53^\circ) = 150 \text{ N}$  &

$$F_{3y} = -250 \text{ N } \sin(53^\circ) = -200 \text{ N}$$

so  $R_x = 50 \text{ N} - 150 \text{ N} = -100 \text{ N}$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\theta = 53^\circ$$

$$\Rightarrow \vec{F}_1 = 50 \text{ N } \hat{j}$$

$$\& \vec{F}_2 = 120 \text{ N } (-\hat{j})$$

$$\& \vec{F}_3 = F_{3x} \hat{i} + F_{3y} \hat{j}$$

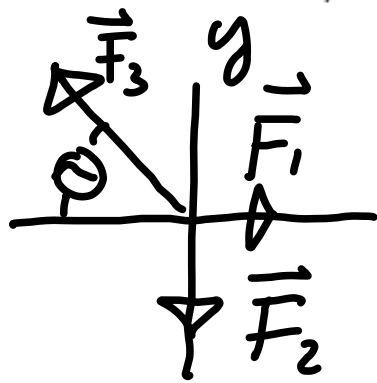
where  $F_{3x} = 250 \text{ N} \cos(53^\circ) = 150 \text{ N}$  &

$$F_{3y} = -250 \text{ N} \sin(53^\circ) = -200 \text{ N}$$

so  $R_x = 50 \text{ N} - 150 \text{ N} = -100 \text{ N}$  &

$$R_y = -120 \text{ N}$$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50$  N,  $F_2 = 120$  N, and  $F_3 = 250$  N. Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\theta = 53^\circ$$

$$\Rightarrow \vec{F}_1 = 50\text{N} \hat{j}$$

$$\& \vec{F}_2 = 120\text{N}(-\hat{j})$$

$$\& \vec{F}_3 = F_{3x} \hat{i} + F_{3y} \hat{j}$$

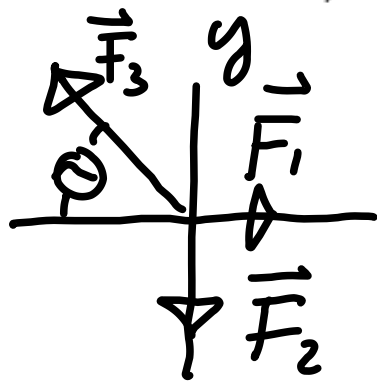
where  $F_{3x} = 250 \text{ N} \cos(53^\circ) = 150 \text{ N}$  &

$$F_{3y} = -250 \text{ N} \sin(53^\circ) = -200 \text{ N}$$

so  $R_x = 50 \text{ N} - 150 \text{ N} = -100 \text{ N}$  &

$$R_y = -120 \text{ N} + 200 \text{ N}$$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\theta = 53^\circ$$

$$\Rightarrow \vec{F}_1 = 50 \text{ N } \hat{i}$$

$$\& \vec{F}_2 = 120 \text{ N } (-\hat{j})$$

$$\& \vec{F}_3 = F_{3x} \hat{i} + F_{3y} \hat{j}$$

where  $F_{3x} = 250 \text{ N } \cos(53^\circ) = 150 \text{ N}$  &

$$F_{3y} = -250 \text{ N } \sin(53^\circ) = -200 \text{ N}$$

so  $R_x = 50 \text{ N} - 150 \text{ N} = -100 \text{ N}$  &

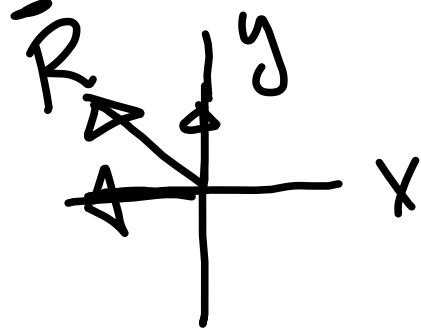
$$R_y = -120 \text{ N} + 200 \text{ N} = 80 \text{ N}$$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50$  N,  $F_2 = 120$  N, and  $F_3 = 250$  N. Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.

$$\text{So } \vec{R} = -100\text{N } \hat{i} + 80\text{N } \hat{j}$$

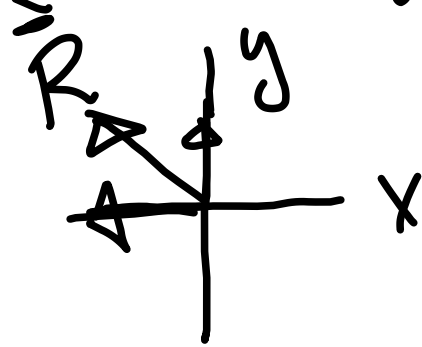
Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50$  N,  $F_2 = 120$  N, and  $F_3 = 250$  N. Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.

Do

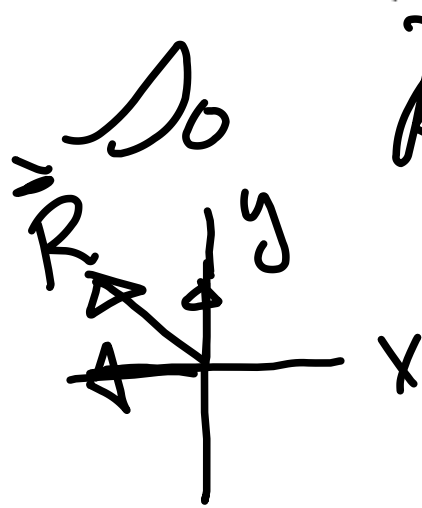

$$\vec{R} = -100\text{N}\hat{i} + 80\text{N}\hat{j}$$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50$  N,  $F_2 = 120$  N, and  $F_3 = 250$  N. Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.

Do


$$\vec{R} = -100\text{N}\hat{i} + 80\text{N}\hat{j}$$
$$R = \sqrt{R_x^2 + R_y^2}$$

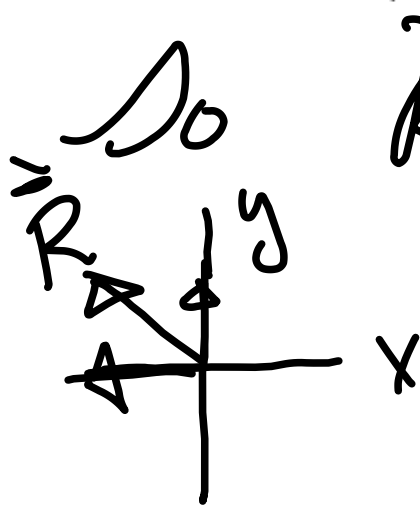
Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50$  N,  $F_2 = 120$  N, and  $F_3 = 250$  N. Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\vec{R} = -100\text{N}\hat{i} + 80\text{N}\hat{j}$$

$$R = \sqrt{R_x^2 + R_y^2}$$
$$= \sqrt{100^2 + 80^2} \text{ N}$$

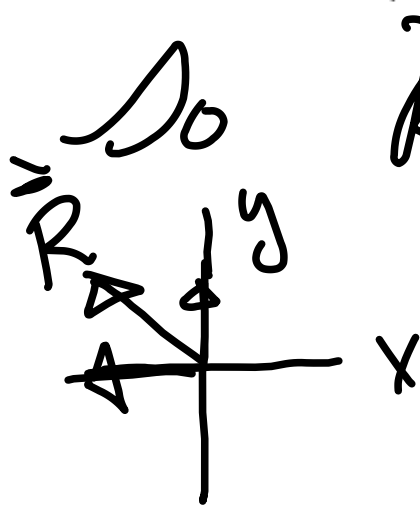
Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\vec{R} = -100\text{N}\hat{i} + 80\text{N}\hat{j}$$

$$\begin{aligned} R &= \sqrt{R_x^2 + R_y^2} \\ &= \sqrt{100^2 + 80^2} \text{ N} = 128 \text{ N} \end{aligned}$$

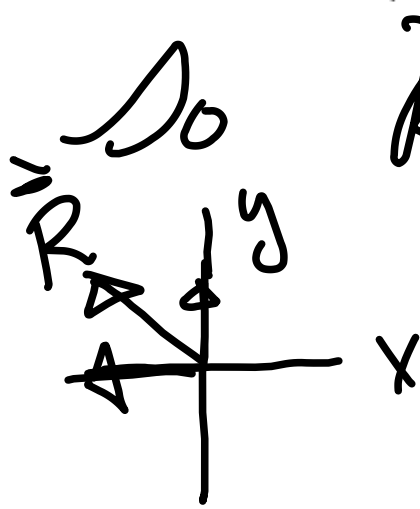
Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\vec{R} = -100\text{N}\hat{i} + 80\text{N}\hat{j}$$

$$R = \sqrt{R_x^2 + R_y^2}$$
$$= \sqrt{100^2 + 80^2} \text{ N} = 128 \text{ N}$$

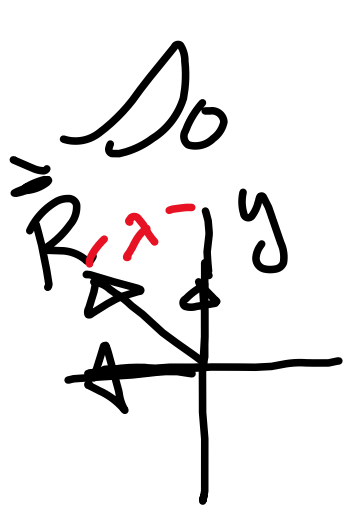
Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50$  N,  $F_2 = 120$  N, and  $F_3 = 250$  N. Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\vec{R} = -100\text{N}\hat{i} + 80\text{N}\hat{j}$$

$$\begin{aligned} R &= \sqrt{R_x^2 + R_y^2} \\ &= \sqrt{100^2 + 80^2} \text{ N} = 128 \text{ N} \end{aligned}$$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.

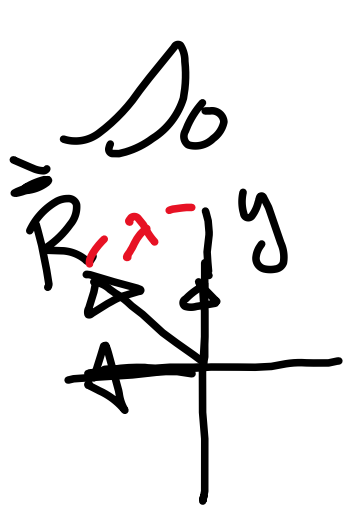


$$\vec{R} = -100\text{N}\hat{i} + 80\text{N}\hat{j}$$

$$R = \sqrt{R_x^2 + R_y^2}$$
$$= \sqrt{100^2 + 80^2} \text{ N} = 128 \text{ N}$$

$$\tan \lambda = \frac{R_x}{R_y}$$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.

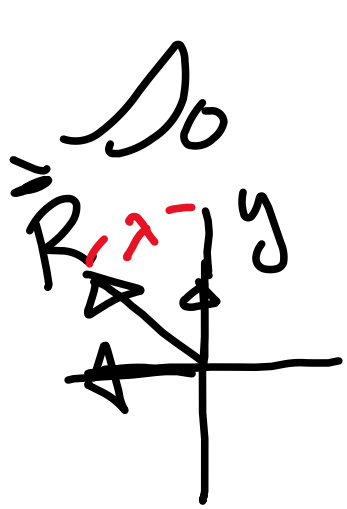


$$\vec{R} = -100\text{N}\hat{i} + 80\text{N}\hat{j}$$

$$R = \sqrt{R_x^2 + R_y^2} \\ = \sqrt{100^2 + 80^2} \text{ N} = 128 \text{ N}$$

$$\tan \lambda = \frac{R_x}{R_y} = \frac{100}{80}$$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.

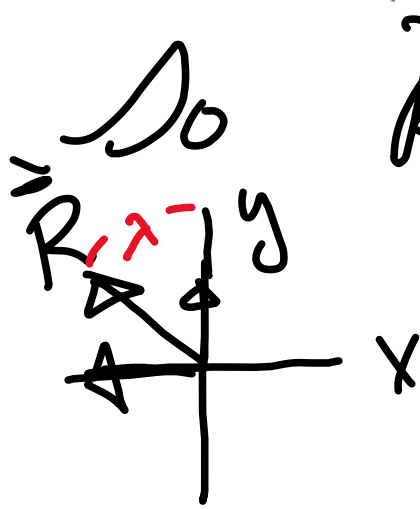


$$\vec{R} = -100\text{N}\hat{i} + 80\text{N}\hat{j}$$

$$R = \sqrt{R_x^2 + R_y^2} \\ = \sqrt{100^2 + 80^2} \text{ N} = 128 \text{ N}$$

$$\tan \lambda = \frac{R_x}{R_y} = \frac{100}{80} \Rightarrow \lambda = \tan^{-1}\left(\frac{100}{80}\right)$$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50$  N,  $F_2 = 120$  N, and  $F_3 = 250$  N. Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\vec{R} = -100\text{N}\hat{i} + 80\text{N}\hat{j}$$

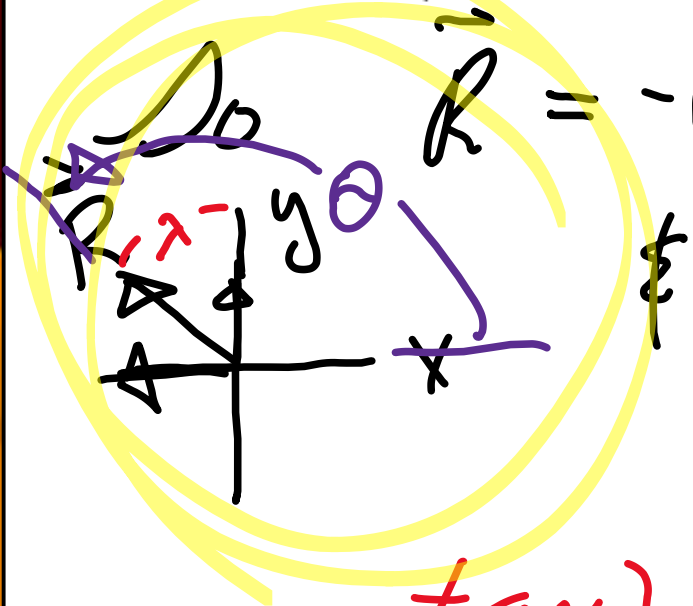
$$R = \sqrt{R_x^2 + R_y^2} \\ = \sqrt{100^2 + 80^2} \text{ N} = 128 \text{ N}$$

$$\tan \lambda = \frac{R_x}{R_y} = \frac{100}{80} \Rightarrow \lambda = \tan^{-1}\left(\frac{100}{80}\right)$$

$$\Rightarrow \lambda = 51^\circ$$



Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\vec{R} = -100\text{N}\hat{i} + 80\text{N}\hat{j}$$

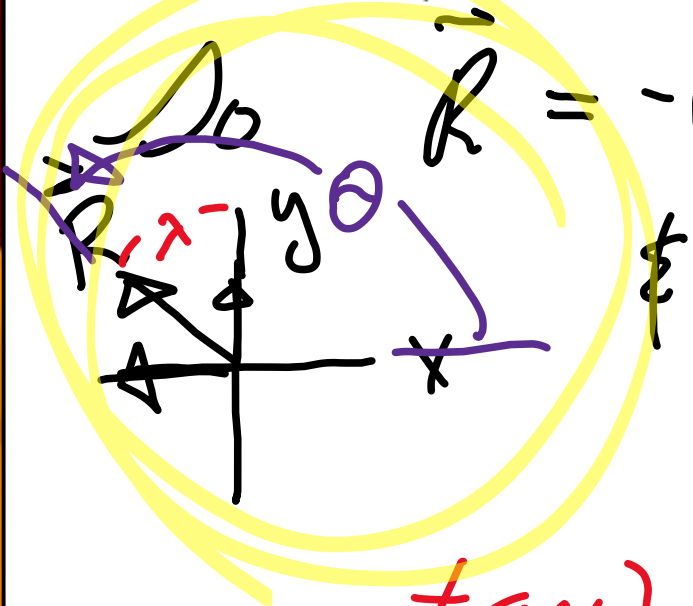
$$R = \sqrt{R_x^2 + R_y^2}$$

$$= \sqrt{100^2 + 80^2} \text{ N} = 128 \text{ N}$$

$$\tan \lambda = \frac{R_x}{R_y} = \frac{100}{80} \Rightarrow \lambda = \tan^{-1}\left(\frac{100}{80}\right)$$

$$\Rightarrow \lambda = 51^\circ \text{ But } \theta = 90^\circ + \lambda$$

Three professional wrestlers are fighting over a champion's belt. Figure 4.7a shows the horizontal force each wrestler applies to the belt, as viewed from above. The forces have magnitudes  $F_1 = 50 \text{ N}$ ,  $F_2 = 120 \text{ N}$ , and  $F_3 = 250 \text{ N}$ . Find the  $x$ - and  $y$ -components of the net force on the belt, and find its magnitude and direction.



$$\vec{R} = -100\text{N}\hat{i} + 80\text{N}\hat{j}$$

$$R = \sqrt{R_x^2 + R_y^2}$$

$$= \sqrt{100^2 + 80^2} \text{ N} = 128 \text{ N}$$

$$\tan \lambda = \frac{R_x}{R_y} = \frac{100}{80} \Rightarrow \lambda = \tan^{-1}\left(\frac{100}{80}\right)$$

$$\Rightarrow \lambda = 51^\circ \text{ But } \theta = 90^\circ + \lambda$$

$$\text{So } \theta = 141^\circ$$

# Newton's First law

# Newton's First law

$$\vec{F} = m\vec{a}$$

# Newton's First law

$$\vec{F} = m\vec{a} \quad \text{so, if}$$

$$\vec{F} = \vec{0}$$

# Newton's First law

$$\vec{F} = m\vec{a} \quad \text{so, if}$$

$$\vec{F} = \emptyset \quad \text{then} \quad \vec{a} = \emptyset$$

# Newton's First law

$$\vec{F} = m\vec{a} \quad \text{so, if}$$

$$\vec{F} = \vec{0} \quad \text{then} \quad \vec{a} = \vec{0} \quad \&$$

$$\vec{v} = \text{constant}$$

# Newton's First law

$$\vec{F} = m\vec{a} \quad \text{so, if}$$

$$\vec{F} = \vec{0} \quad \text{then} \quad \vec{a} = \vec{0} \quad \&$$

$$\vec{v} = \text{constant}$$

No force  $\Rightarrow$  constant velocity

# Newton's First law

$$\vec{F} = m\vec{a} \quad \text{so, if}$$

$$\vec{F} = \vec{0} \quad \text{then} \quad \vec{a} = \vec{0} \quad \&$$

$$\vec{v} = \text{constant}$$

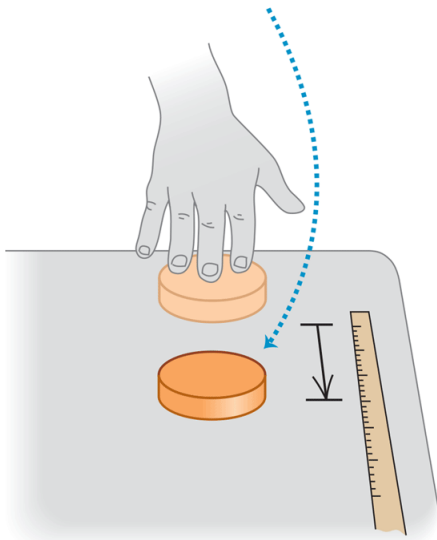
No force  $\Rightarrow$  constant velocity

Net force  $\Rightarrow$  acceleration

# Motion of disk on different surfaces

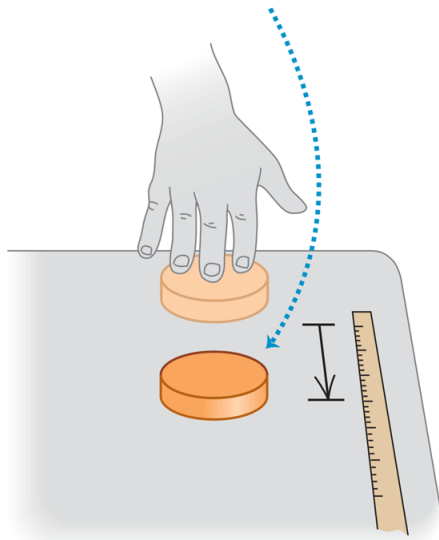
# Motion of disk on different surfaces

(a) Table: puck stops short.

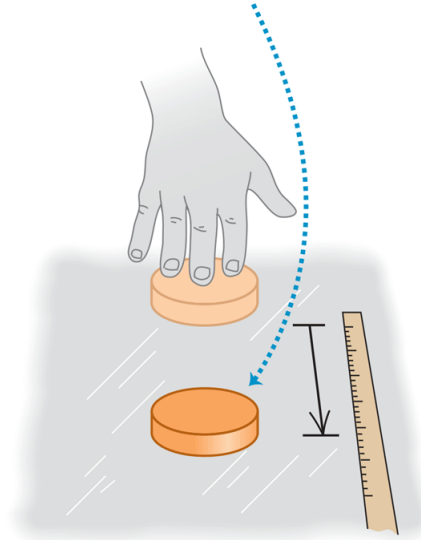


# Motion of disk on different surfaces

(a) Table: puck stops short.

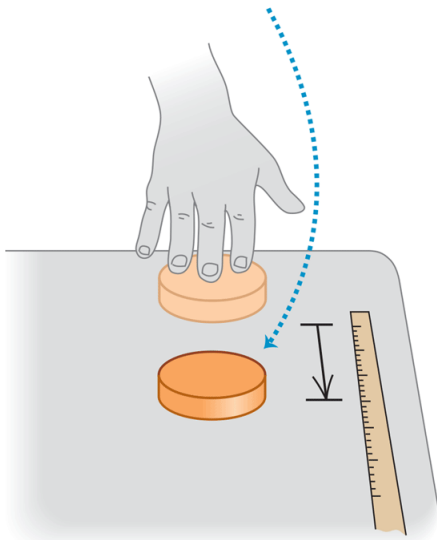


(b) Ice: puck slides farther.

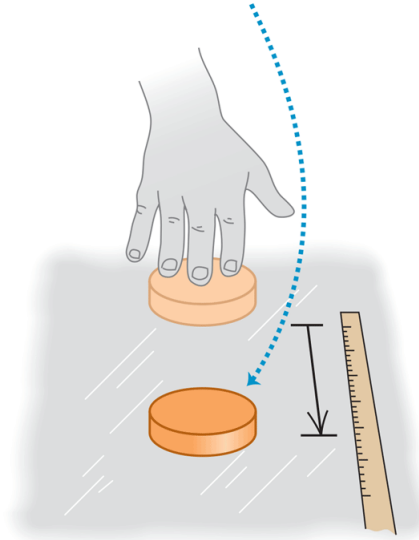


# Motion of disk on different surfaces

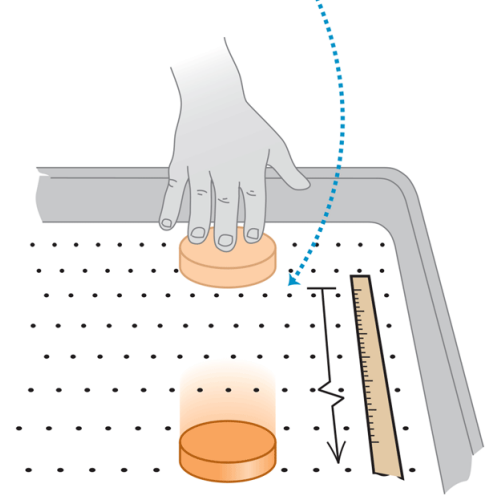
(a) Table: puck stops short.



(b) Ice: puck slides farther.

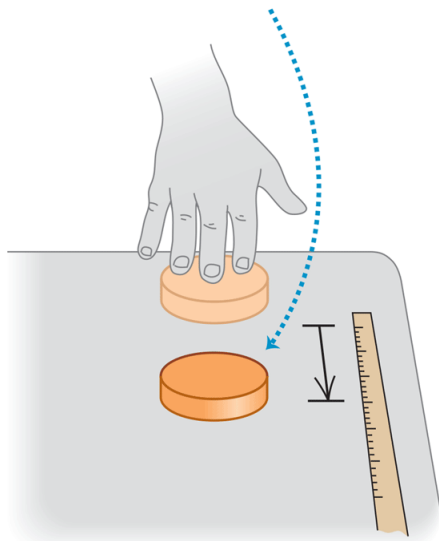


(c) Air-hockey table: puck slides even farther.

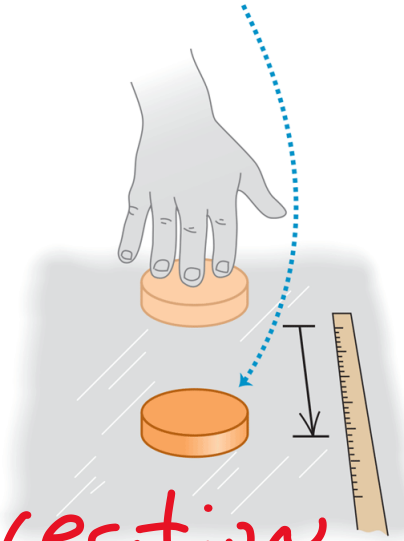


# Motion of disk on different surfaces

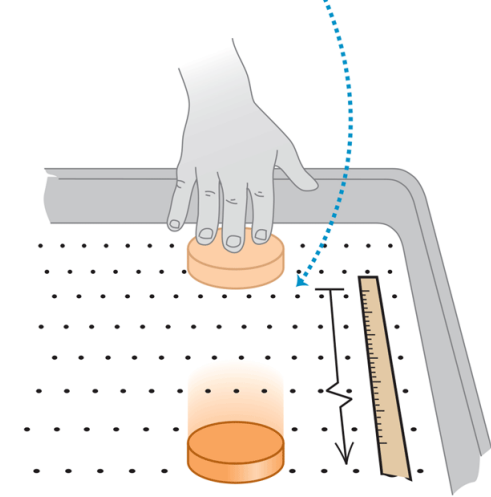
(a) Table: puck stops short.



(b) Ice: puck slides farther.



(c) Air-hockey table: puck slides even farther.



Direction of

Less frictional force

opposing the motion of disk

# Newton's First law

$$\vec{F} = m\vec{a} \quad \leftarrow \text{mathematical form}$$

# Newton's First law

$$\vec{F} = m\vec{a}$$

word form  
↓

## **Newton's first law of motion**

An object acted on by no net external force has a constant velocity (which may be zero) and zero acceleration

# Newton's First law

$$\vec{F} = m\vec{a}$$

## **Newton's first law of motion**

An object acted on by no net external force has a constant velocity (which may be zero) and zero acceleration

Inertia  $\equiv$  Tendency of an object to keep moving once it is in motion

# Inertial frame

An inertial frame of reference is a reference frame where  $\vec{F} = m\vec{a}$  is valid.

# Inertial frame

An inertial frame of reference is a reference frame where  $\vec{F} = m\vec{a}$  is valid.

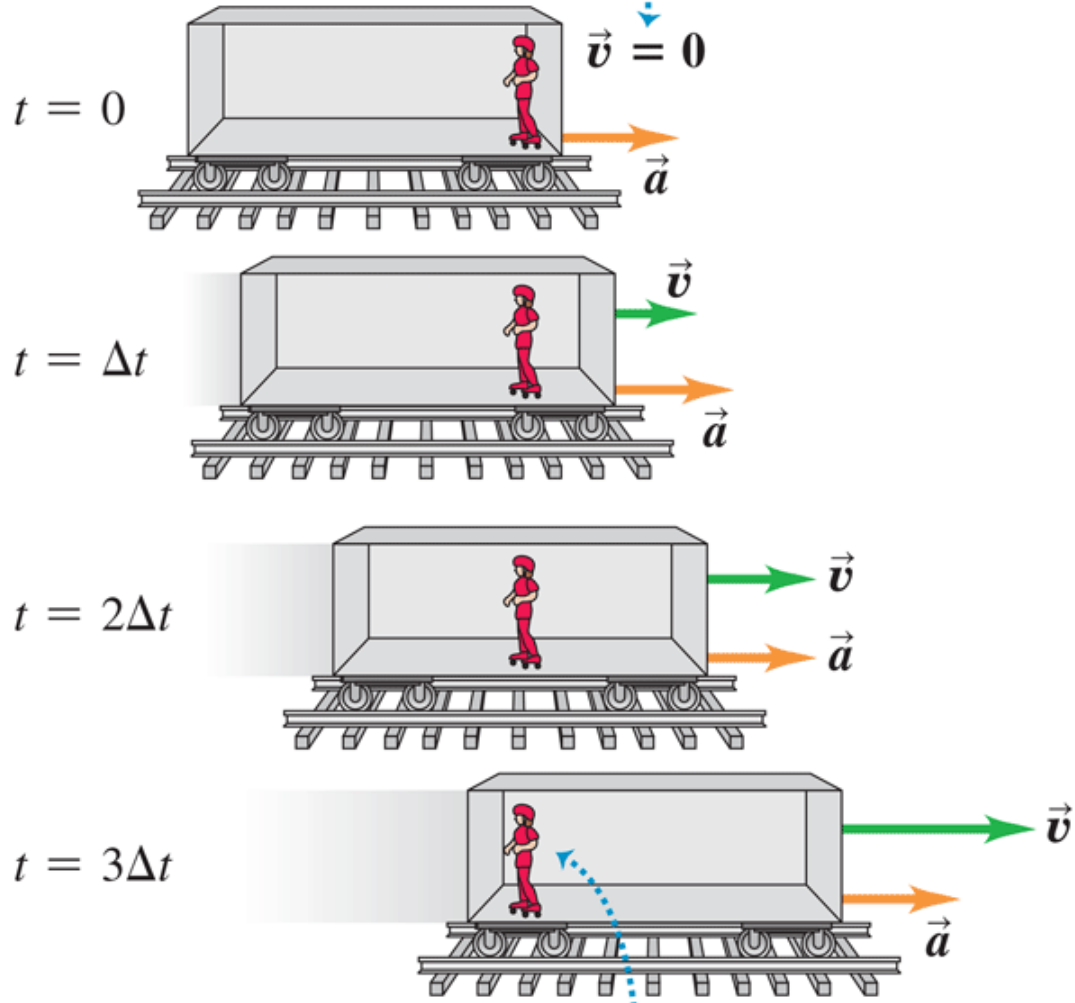
A non inertial frame is just a frame that is itself accelerating

# Inertial frame

An inertial frame of reference is a reference frame where  $\vec{F} = m\vec{a}$  is valid.

A non inertial frame is just a frame that is itself accelerating → messes up  $\vec{F} = m\vec{a}$  since there is acceleration of the frame not being accounted for

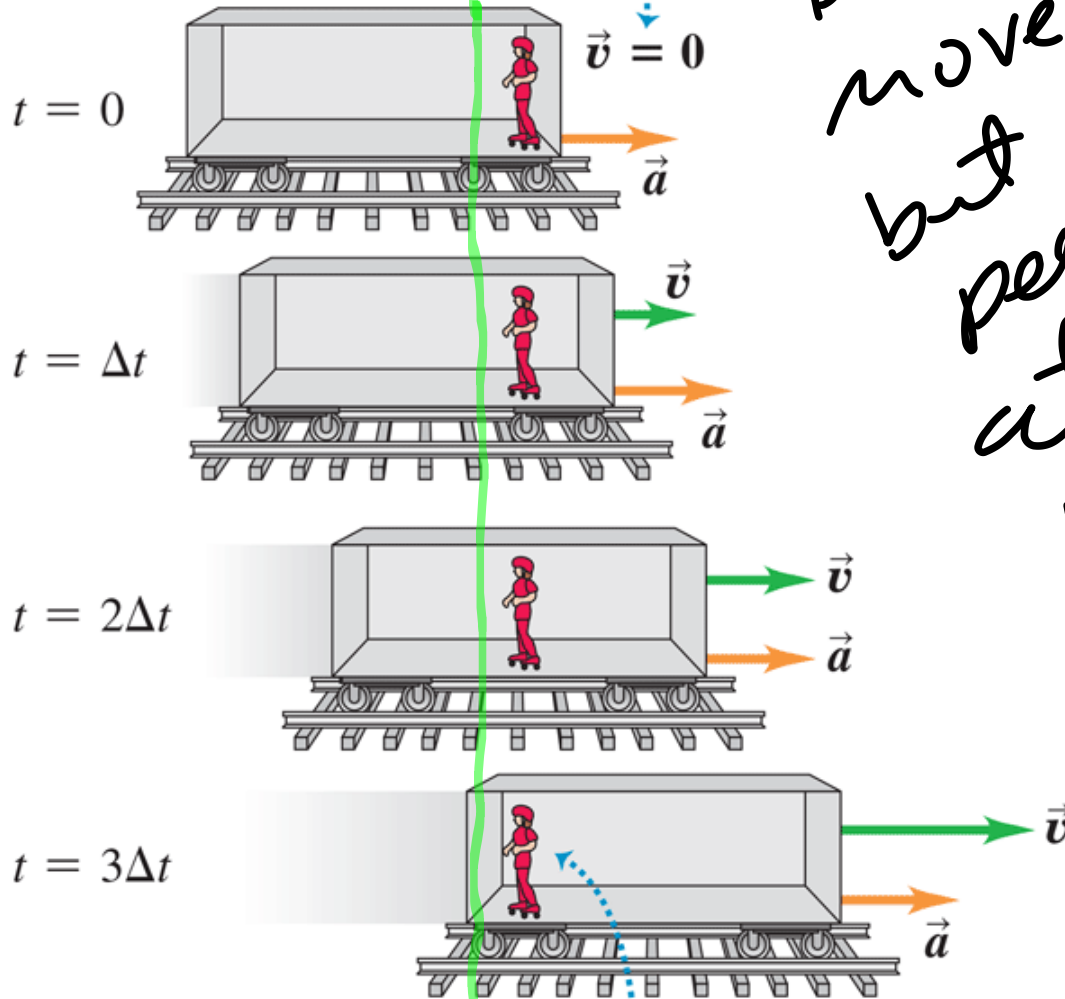
(a) Initially, you and the vehicle are at rest.



You tend to remain at rest as the vehicle accelerates around you.



(a) Initially, you and the vehicle are at rest.

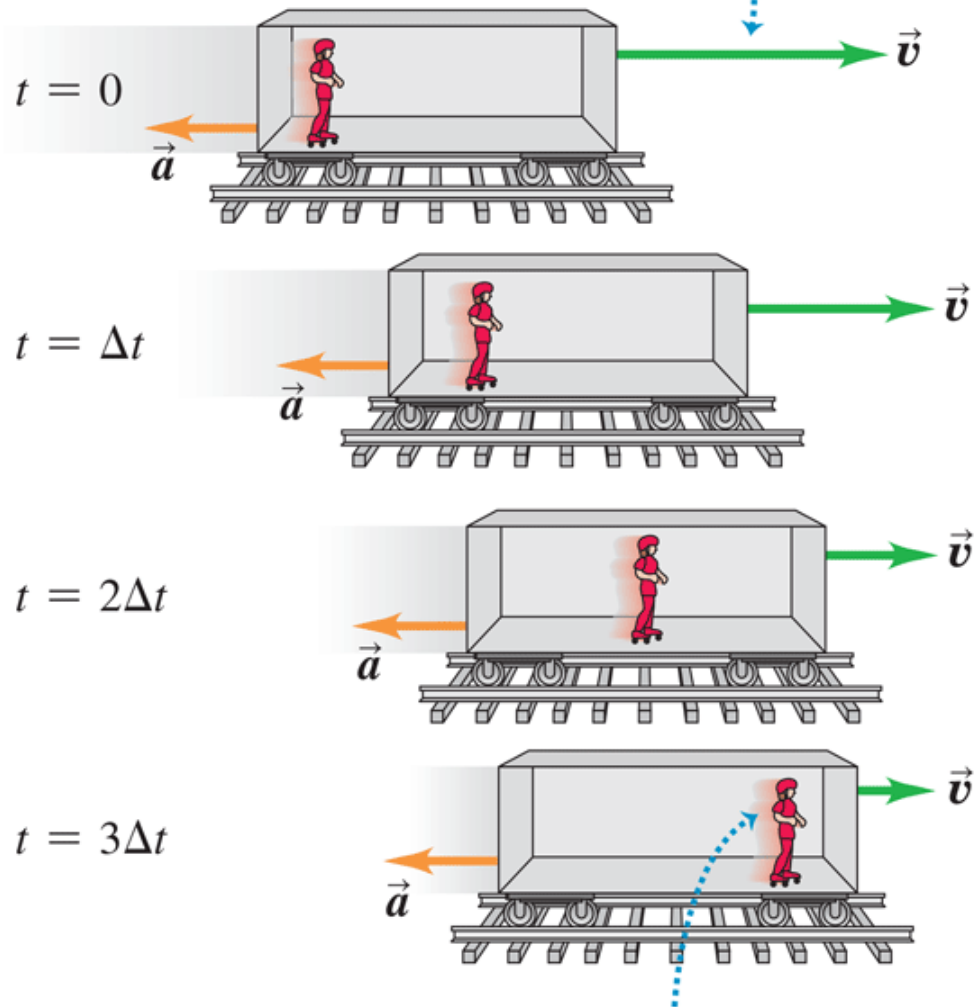


Box moves  
but  
person  
at  
rest

You tend to remain at rest as the vehicle accelerates around you.

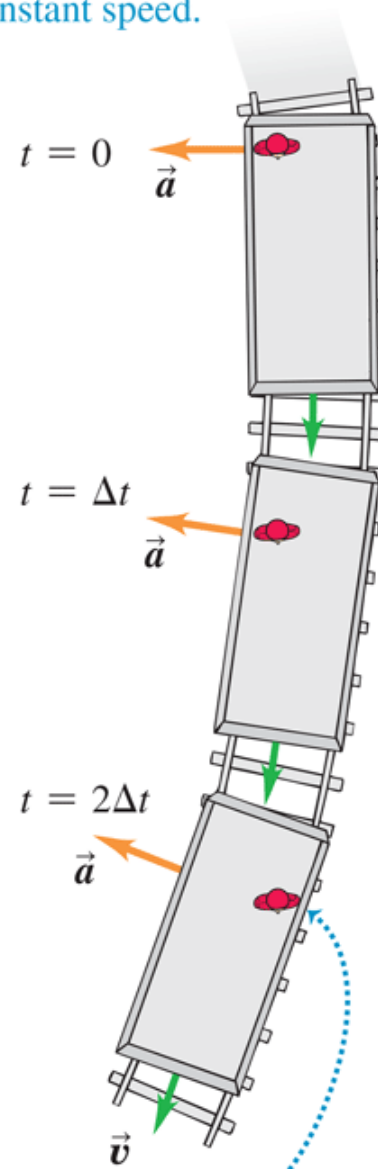
(b)

Initially, you and the vehicle are in motion.



You tend to continue moving with constant velocity as the vehicle slows down around you.

- (c) The vehicle rounds a turn at constant speed.



You tend to continue moving in a straight line as the vehicle turns.



